Package 'gRbase'

November 29, 2023

```
Version 2.0.1
Title A Package for Graphical Modelling in R
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Description The 'gRbase' package provides graphical modelling features
     used by e.g. the packages 'gRain', 'gRim' and 'gRc'. 'gRbase' implements
     graph algorithms including (i) maximum cardinality search (for marked
     and unmarked graphs).
     (ii) moralization, (iii) triangulation, (iv) creation of junction tree.
     'gRbase' facilitates array operations,
     'gRbase' implements functions for testing for conditional independence.
     'gRbase' illustrates how hierarchical log-linear models may be
     implemented and describes concept of graphical meta
     data.
     The facilities of the package are documented in the book by Højsgaard,
     Edwards and Lauritzen (2012,
     <doi:10.1007/978-1-4614-2299-0>) and in the paper by
     Dethlefsen and Højsgaard, (2005, <doi:10.18637/jss.v014.i17>).
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```

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all_pairs

Create all possible pairs

Description

Create all possible pairs of two character vectors.

Usage

Index

```
all_pairs(x, y = character(0), sort = FALSE, result = "matrix")
names2pairs(x, y = NULL, sort = TRUE, result = "list")
```

Arguments

x, y Character vectors.

sort Logical.

result A list or a matrix.

Details

NOTICE: If y is not NULL then x and y must be disjoint (no checks are made); otherwise pairs of identical elements wil also be obtained.

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Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
x <- letters[1:4]
y <- letters[5:7]

all_pairs(x)
all_pairs(x, result="matrix")

all_pairs(x, y)
all_pairs(x, y, result="matrix")</pre>
```

all_subsets

Create all subsets

Description

Create all subsets of a vector

Usage

```
all_subsets(x)
all_subsets0(x)
```

Arguments

Χ

Vector

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

api-array-07

Array operations (2007)

Description

Array operations; created to facilitate the gRain package in 2007. Now largely replaceable by other (often faster) functions implemented in Rcpp.

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Usage

```
tablePerm(tab, perm, resize = TRUE, keep.class = FALSE)
tableMult(tab1, tab2)
tableOp(tab1, tab2, op = "*")
tableOp2(tab1, tab2, op = `*`, restore = FALSE)
tableOp0(tab1, tab2, op = `*`)
tableSlice(tab, margin, level, impose)
tableSlicePrim(tab, mar.idx, lev.idx)
tableMargin(tab, margin, keep.class = FALSE)
tableGetSliceIndex(tab, margin, level, complement = FALSE)
tableSetSliceValue(tab, margin, level, complement = FALSE, value = 0)
```

Arguments

tab, tab1, tab2 Arrays with named dimnames.

perm A permutation; either indices or names.

resize A flag indicating whether the vector should be resized as well as having its

elements reordered (default TRUE).

keep.class Obsolete argument.

op The operation; choices are "*", "/", "+", "-".

restore Not so clear anymore.

margin Index or name of margin.

level Corresponding level of margin.

impose Value to be imposed.

mar.idx Index of margin
lev.idx Index of level

complement Should values be set for the complement?

value Which value should be set

Details

tableOp0 is brute force implementation based on dataframes. It is very slow, but useful for error checking.

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```
api-array-properties Check if object is array
```

Description

Check if object is array (that it is a vector with a dim attribute) and that the object has dimnames and that dimnames are named.

Usage

```
is.named.array(obj)
is_named_array_(obj)
is_number_vector_(obj)
is_dimnames_(obj)
dimnames_match(a1, a2)
```

Arguments

```
obj Some R object.
a1, a2 Arrays with named dimnames.
```

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

```
is.named.array( HairEyeColor )
is.named.array( matrix(1:4, nrow=2) )
is_named_array_( HairEyeColor )
is_named_array_( matrix(1:4, nrow=2) )
is_number_vector_(1:4)
is_number_vector_(list(1:4))

ar1 = tabNew(c("a", "b"), levels=c(2, 3))
ar2 = tabNew(c("c", "a"), levels=c(2, 2))
ar1
ar2
## dimension a has levels a1,a2 in both ar1 and ar2.
# Hence we have a match.
dimnames_match(ar1, ar2)

ar1 = tabNew(c("a", "b"), levels=c(2, 3))
ar2 = tabNew(c("c", "a"), levels=c(2, 3))
ar1
```

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```
ar2
## dimension a has levels a1,a2 in ar1 and levels a1,a2,a3 in ar2.
# Hence we do not have a match.
dimnames_match(ar1, ar2)

ar2 = tabNew(c("c", "a"), levels=list(c=c("c1", "c2"), a=c("a2", "a1")))
ar2
## dimension a has levels a1,a2 in ar1 and levels a2,a1 in ar2.
# Hence we do not have a match.
dimnames_match(ar1, ar2)
```

api-cell

Table cell operations.

Description

Low level table cell operations.

Usage

```
cell2entry(cell, dim)
entry2cell(entry, dim)

next_cell(cell, dim)

next_cell2(cell, dim)

next_cell_slice(cell, dim, slice_marg)

slice2entry(slice_cell, slice_marg, dim)

cell2entry_perm(cell, dim, perm)

perm_cell_entries(perm, dim)

fact_grid(dim, slice_cell = NULL, slice_marg = NULL)
```

Arguments

cell	Vector giving the cell, e.g. c(1, 1, 2) in 3-way table.
dim	Vector giving array dimension, eg c(2, 2, 2).
entry	An entry in an array (a number indexing a vector).
slice_marg	Vector giving the margin of a table, eg. c(2, 3)
slice_cell	Vector giving the corresponding cell of marginal table, e.g. c(1, 2)
perm	Vector giving permutaion of array, eg. c(1, 3, 2).

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Examples

```
di <- c(2, 2, 3)
cell2entry(c(1, 1, 1), dim=di)
cell2entry(c(2, 2, 3), dim=di)
entry2cell(1, dim=di)
entry2cell(12, dim=di)
next_cell(c(1, 1, 1), dim=di)
next_cell(c(2, 1, 1), dim=di)
## The first two entries are kept fixed
next_cell_slice(c(2, 1, 1), dim=di, slice_marg=c(1, 2))
next_cell_slice(c(2, 1, 2), dim=di, slice_marg=c(1, 2))
## Cell (2, 2, 1) corresponds to entry 4
cell2entry(c(2, 2, 1), dim=di)
## Same as
cell2entry_perm(c(2, 2, 1), dim=di, perm=c(1, 2, 3))
## If the table dimensions are permuted as (3, 1, 2)
## the entry becomes
cell2entry_perm(c(2, 2, 1), dim=di, perm=c(3, 1, 2))
```

api-cell_

Low level table cell operations implemented in c++

Description

Corresponding R functions without the trailing underscore exist.

Usage

```
cell2entry_(cell, dim)
make_plevels_(dim)
entry2cell_(entry, dim)
next_cell_(cell, dim)
next_cell2_(cell, dim)
next_cell_slice_(cell, dim, slice_marg)
slice2entry_(slice_cell, slice_marg, dim)
```

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```
cell2entry_perm_(cell, dim, perm)
perm_cell_entries_(perm, dim)
```

Arguments

Vector giving the cell, e.g. $c(1, 1, 2)$ in 3-way table.	
dim Vector giving array dimension, eg $c(2, 2, 2)$.	
entry An entry in an array (a number indexing a vector).	
slice_marg Vector giving the margin of a table, eg. c(2, 3)	
slice_cell	Vector giving the corresponding cell of marginal table, e.g. $c(1, 2)$
perm Vector giving permutaion of array, eg. c(1, 3, 2).	

api-parray

Representation of and operations on multidimensional arrays

Description

General representation of multidimensional arrays (with named dimnames, also called named arrays.)

Usage

```
parray(varNames, levels, values = 1, normalize = "none", smooth = 0)
as.parray(values, normalize = "none", smooth = 0)
data2parray(data, varNames = NULL, normalize = "none", smooth = 0)
makeDimNames(varNames, levels, sep = "")
```

Arguments

varNames	Names of variables defining table; can be a right hand sided formula.
levels	Either 1) a vector with number of levels of the factors in varNames or 2) a list with specification of the levels of the factors in varNames. See 'examples' below.
values	Values to go into the array
normalize	Either "none", "first" or "all". Should result be normalized, see 'Details' below.
smooth	Should values be smoothed, see 'Details' below.
data	Data to be coerced to a parray; can be data.frame, table, xtabs, matrix.
sep	Desired separator in dim names; defaults to "".

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Details

A named array object represents a table defined by a set of variables and their levels, together with the values of the table. E.g. f(a,b,c) can be a table with a,b,c representing levels of binary variable

If normalize="first" then for each configuration of all other variables than the first, the probabilities are normalized to sum to one. Thus f(a,b,c) becomes a conditional probability table of the form p(alb,c).

If normalize="all" then the sum over all entries of f(a,b,c) is one.

If smooth is positive then smooth is added to values before normalization takes place.

Value

A a named array.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
is.named.array
```

```
t1 <- parray(c("gender", "answer"), list(c('male', 'female'),c('yes', 'no')), values=1:4)
t1 <- parray(~gender:answer, list(c('male','female'),c('yes','no')), values=1:4)
t1 <- parray(~gender:answer, c(2,2), values=1:4)
t2 <- parray(c("answer", "category"), list(c('yes', 'no'), c(1,2)), values=1:4+10)
t3 <- parray(c("category", "foo"), c(2,2), values=1:4+100)
varNames(t1)
nLevels(t1)
valueLabels(t1)
## Create 1-dimensional vector with dim and dimnames
x1 <- 1:5
as.parray(x1)
x2 <- parray("x", levels=length(x1), values=x1)</pre>
dim(x2)
dimnames(x2)
## Matrix
x1 <- matrix(1:6, nrow=2)</pre>
as.parray(x1)
parray(~a:b, levels=dim(x1), values=x1)
## Extract parrays from data
## 1) a dataframe
data(cad1)
```

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```
data2parray(cad1, ~Sex:AngPec:AMI)
data2parray(cad1, c("Sex","AngPec","AMI"))
data2parray(cad1, c(1,2,3))
## 2) a table
data2parray(UCBAdmissions,c(1,2), normalize="first")
```

api-pct-operations

Array algebra

Description

Addition, subtraction etc. of arrays

Usage

a1 %a+% a2

a1 %a-% a2

a1 %a*% a2

a1 %a/% a2

a1 %a/0% a2

tab1 %a_% marg

tab1 %a==% tab2

tab1 %a^% extra

tab1 %aperm% perm

tab1 %aalign% tab2

tab1 %aslice% slice

tab1 %aslice*% slice

tab1 %amarg% marg

Arguments

tab1, tab2 Multidimensional arrays with named dimnames (we call them 'named arrays').

marg A vector of indices or dimnames or a right hand sided formula giving the desired

marginal.

extra List defining the extra dimensions.

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perm	A vector of indices or dimnames or a right hand sided formula giving the desired
	permutiation.
slice	A list of the form name=value.
a, a1, a2	Arrays (with named dimnames)

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
hec <- HairEyeColor
a1 <- tabMarg(hec, c("Hair", "Eye"))
a2 <- tabMarg(hec, c("Hair", "Sex"))
a3 <- tabMarg(hec, c("Eye", "Sex"))

## Binary operations
a1 %a+% a2
a1 %a-% a2
a1 %a-% a2
a1 %a-% a2
a1 %a-% a2
```

api-tabDist

Marginalize and condition in multidimensional array.

Description

Marginalize and condition in a multidimensional array which is assumed to represent a discrete multivariate distribution.

Usage

```
tabDist(tab, marg = NULL, cond = NULL, normalize = TRUE)
```

Arguments

tab	Multidimensional array with dimnames.
marg	A specification of the desired margin; a character vector, a numeric vector or a right hand sided formula.
cond	A specification of what is conditioned on. Can take two forms: Form one is a a character vector, a numeric vector or a right hand sided formula. Form two is as a simple slice of the array, which is a list of the form var1=value1, var2=value2 etc.
normalize	Should the result be normalized to sum to 1.

Value

A multidimensional array.

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Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

```
hec <- HairEyeColor
is.named.array( hec )
## We need dimnames, and names on the dimnames
## Marginalize:
tabDist(hec, marg= ~Hair + Eye)
tabDist(hec, marg= ~Hair:Eye)
tabDist(hec, marg= c("Hair", "Eye"))
tabDist(hec, marg= 1:2)
tabDist(hec, marg= ~Hair + Eye, normalize=FALSE)
## Condition
tabDist(hec, cond= ~Sex + Hair)
tabDist(hec, cond= ~Sex:Hair)
tabDist(hec, cond= c("Sex", "Hair"))
tabDist(hec, cond = c(3,1))
tabDist(hec, cond= list(Hair="Black"))
tabDist(hec, cond= list(Hair=1))
## Not run:
## This will fail
tabDist(hec, cond= list(Hair=c("Black", "Brown")))
tabDist(hec, cond= list(Hair=1:2))
## End(Not run)
## But this will do the trick
a <- tabSlice(hec, slice=list(Hair=c("Black", "Brown")))</pre>
tabDist(a, cond=~Hair)
## Combined
tabDist(hec, marg=~Hair+Eye, cond=~Sex)
tabDist(hec, marg=~Hair+Eye, cond="Sex")
tabDist(hec, marg=~Hair+Eye, cond=list(Sex="Male"))
tabDist(hec, marg=~Hair+Eye, cond=list(Sex="Male"), normalize=FALSE)
tabDist(hec, cond=list(Sex="Male"))
tabDist(hec, cond=list(Sex="Male"), normalize=FALSE)
```

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api-tabNew	
api tabiyew	

Create multidimensional arrays

Description

Alternative ways of creating arrays

Usage

```
tabNew(names, levels, values, normalize = "none", smooth = 0)
```

Arguments

names	Names of variables defining table; either a character vector or a right hand sided formula.
levels	1. a list with specification of the levels of the factors in names or 2) a vector with number of levels of the factors in names. See 'examples' below.
values	values to go into the array.
normalize	Either "none", "first" or "all". Should result be normalized, see 'Details' below.
smooth	Should values be smoothed, see 'Details' below.

Details

- 1. If normalize="first" then for each configuration of all other variables than the first, the probabilities are normalized to sum to one. Thus f(a, b, c) becomes a conditional probability table of the form p(a | b, c).
- 2. If normalize="all" then the sum over all entries of f(a,b,c) is one.
- 3. If smooth is positive then smooth is added to values BEFORE normalization takes place.

Value

An array.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

api-tabX

```
t3 <- tabNew(~gender:answer, c(2, 2), values=1:4) t3
```

api-tabX

Interface - operations on multidimensional arrays.

Description

Interface functions and minor extensions to cpp functions.

Usage

```
tabAdd(tab1, tab2)
tabAlign(tab1, tab2)
tabDiv(tab1, tab2)
tabDiv0(tab1, tab2)
tabOp(tab1, tab2, op = "*")
tabEqual(tab1, tab2, eps = 1e-12)
tabExpand(tab, aux, type = 0L)
tabMult(tab1, tab2)
tabSubt(tab1, tab2)
tabListMult(lst)
tabListAdd(lst)
tabPerm(tab, perm)
tabMarg(tab, marg = NULL)
tabSum(tab, ...)
tabProd(tab, ...)
tabNormalize(tab, type = "none")
```

Arguments

ор

The algebraic operation to be carried out.

api-tabX_

```
eps Criterion for checking equality of two arrays.

tab, tab1, tab2, ...

Arrays with named dimnames (we call them 'named arrays').

aux Either a list with names and dimnames or a named array from which such a list can be extracted.

type If 0 then entries are duplicated. If 3 then averages are computed. If 2 then 0 slices are inserted.

lst List of arrays.

perm, marg A vector of indices or dimnames or a right hand sided formula giving the desired permutation/margin.
```

api-tabX_

Table operations implemented in c++

Description

Table operations implemented in c++. Corresponding R functions without the trailing underscore exist.

Usage

```
tab_perm_(tab, perm)
tab_expand_(tab, aux, type = 0L)
tab_align_(tab1, tab2)
tab_marg_(tab, marg)
tab_op_(tab1, tab2, op = "*")
tab_add_(tab1, tab2)
tab_subt_(tab1, tab2)
tab_mult_(tab1, tab2)
tab_div_(tab1, tab2)
tab_div0_(tab1, tab2)
tab_div0_(tab1, tab2)
tab_list_mult_(lst)
tab_list_add_(lst)
```

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Arguments

tab, tab1, tab2	Tables (arrays)
perm, marg	A vector of indices or dimnames or a right hand sided formula giving the desired permutation/margin.
aux	Either a list with names and dimnames or a named array from which such a list can be extracted.
type	If 0 then entries are duplicated. If 3 then averages are computed. If 2 then 0 slices are inserted.
ор	The operation to be carried out; "+", "-", "*", "/".
eps	Criterion for checking equality of two arrays.
lst	List of arrays.

api_tabSlice

Array slices

Description

Functions for extracting slices of arrays

Usage

```
tabSlice(
  tab,
  slice = NULL,
  margin = names(slice),
  drop = TRUE,
  as.array = FALSE
)

tabSlice2(tab, slice, margin.idx, drop = TRUE, as.array = FALSE)

tabSlicePrim(tab, slice, drop = TRUE)

tabSliceMult(tab, slice, val = 1, comp = 0)

tabSlice2Entries(tab, slice, complement = FALSE)
```

Arguments

tab An array with named dimnames.

slice A list defining the slice.

margin Names of variables in slice.

drop If TRUE then dimensions with only one level will be dropped from the output.

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as.array If the resulting array is one-dimensional the result will by default be a vector with no dim attribute unless as.array is TRUE.

margin.idx Indec of variables in slice.

val The values that entries in the slice will be multiplied with.

comp The values that entries NOT in the slice will be multiplied with.

complement If TRUE the complement of the entries are returned.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
x = HairEyeColor
s = list(Hair=c("Black", "Brown"), Eye=c("Brown", "Blue"))
s1 = tabSlice(x, slice=s); s1
tabSlice2Entries(x, slice=s)
tabSlice2Entries(x, slice=s, complement=TRUE)
## tabSliceMult
s2 = tabSliceMult(x, slice=s); s2
sp = list(c(1,2), c(1,2), TRUE)
tabSlicePrim(x, slice=sp)
tabSlice(x, slice=s)
```

array-simulate

Simulate data from array.

Description

Simulate data (slice of) an array: Simulate n observations from the array x conditional on the variables in margin (a vector of indices) takes values given by margin.value

Usage

```
simulateArray(x, nsim = 1, margin, value.margin, seed = NULL)
## S3 method for class 'table'
simulate(object, nsim = 1, seed = NULL, margin, value.margin, ...)
## S3 method for class 'xtabs'
simulate(object, nsim = 1, seed = NULL, margin, value.margin, ...)
## S3 method for class 'array'
simulate(object, nsim = 1, seed = NULL, margin, value.margin, ...)
```

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Arguments

```
x, object An array.

nsim Number of cases to simulate.

margin, value.margin
Specification of slice of array to simulate from.

seed Seed to be used for random number generation.

... Additional arguments, currently not used.
```

Value

A matrix.

Note

The current implementation is fragile in the sense that it is not checked that the input argument x is an array.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

```
## 2x2 array
x <- parray(c("a", "b"), levels=c(2, 2), values=1:4)

## Simulate from entire array
s <- simulateArray(x, 1000)
xtabs(~., as.data.frame(s))

## Simulate from slice defined by that dimension 1 is fixed at level 2
s <-simulateArray(x, 6000, 1, 2)
xtabs(~., as.data.frame(s))

## 2 x 2 x 2 array
x <- parray(c("a", "b", "c"), levels=c(2, 2, 2), values=1:8)
## Simulate from entire array
s <-simulateArray(x, 36000)
xtabs(~., as.data.frame(s))

## Simulate from slice defined by that dimension 3 is fixed at level 1
s <-simulateArray(x, 10000, 3, 1)
xtabs(~., as.data.frame(s))</pre>
```

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compareModels

Generic function for model comparison

Description

compareModels is a generic functions which invoke particular methods which depend on the class of the first argument

Usage

```
compareModels(object, object2, ...)
```

Arguments

```
object, object2

Model objects

Additional arguments
```

Value

The value returned depends on the class of the first argument.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

cov2pcor

Partial correlation (matrix)

Description

cov2pcor calculates the partial correlation matrix from an (empirical) covariance matrix while conc2pcor calculates the partial correlation matrix from a concentration matrix (inverse covariance matrix).

Usage

```
cov2pcor(V)
conc2pcor(K)
```

Arguments

V Covariance matrix
K Concentration matrix

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Value

A matrix with the same dimension as V.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
data(math)
S <- cov.wt(math)$cov
cov2pcor(S)</pre>
```

dag2chol

Create regression matrix matrix from DAG A DAG can be represented as a triangular matrix of regression coefficients.

Description

Create regression matrix matrix from DAG A DAG can be represented as a triangular matrix of regression coefficients.

Usage

```
dag2chol(object)
```

Arguments

object

A graph, either a graphNEL or an igraph object.

```
g \leftarrow dag(x2|x1 + x3|x1:x2 + x4|x3)

dag2chol(g)
```

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data-ashtrees

Crown dieback in ash trees

Description

This dataset comes from a study of symptoms of crown dieback, cankers and symptoms caused by other pathogens and pests in ash trees (Fraxinus excelsior). In all 454 trees were observed in two plots. There are 8 categorical variables, 6 of which are binary and two are trichotomous with values representing increasing severity of symptoms, and one continuous variable, tree diameter at breast height (DBH).

Usage

```
data(ashtrees)
```

Format

A data frame with 454 observations on the following 9 variables.

```
plot a factor with levels 2 6
dieback a factor with levels 0 1 2
dead50 a factor with levels 0 0.5 1
bushy a factor with levels 0 1
canker a factor with levels BRNCH MAIN NONE
wilt a factor with levels 0 1
roses a factor with levels 0 1
discolour a factor with levels 0 1
dbh a numeric vector
```

References

Skovgaard JP, Thomsen IM, Skovgaard IM and Martinussen T (2009). Associations among symptoms of dieback in even-aged stands of ash (Fraxinus excelsior L.). Forest Pathology.

```
data(ashtrees)
head(ashtrees)
```

data-BodyFat 23

data-BodyFat	Body Fat Data	
--------------	---------------	--

Description

Estimates of the percentage of body fat determined by underwater weighing and various body circumference measurements for 252 men.

Usage

```
data(BodyFat)
data(BodyFat)
```

Format

A data frame with 252 observations on the following 15 variables.

Density Density determined from underwater weighing, a numeric vector

BodyFat Percent body fat from Siri's (1956) equation, a numeric vector

Age in years, a numeric vector

Weight in lbs, a numeric vector

Height in inches, a numeric vector

Neck circumference in cm, a numeric vector

Chest circumference in cm, a numeric vector

Abdomen circumference in cm, a numeric vector

Hip circumference in cm, a numeric vector

Thigh circumference in cm, a numeric vector

Knee circumference in cm. a numeric vector

Ankle circumference in cm, a numeric vector

Biceps circumference in cm, a numeric vector

Forearm circumference in cm, a numeric vector

Wrist circumference in cm, a numeric vector

Source

For more information see https://lib.stat.cmu.edu/datasets/bodyfat

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References

Bailey, Covert (1994). *Smart Exercise: Burning Fat, Getting Fit*, Houghton-Mifflin Co., Boston, pp. 179-186.

Behnke, A.R. and Wilmore, J.H. (1974). Evaluation and Regulation of Body Build and Composition, Prentice-Hall, Englewood Cliffs, N.J.

Siri, W.E. (1956), "Gross composition of the body", in *Advances in Biological and Medical Physics*, vol. IV, edited by J.H. Lawrence and C.A. Tobias, Academic Press, Inc., New York.

Katch, Frank and McArdle, William (1977). *Nutrition, Weight Control, and Exercise*, Houghton Mifflin Co., Boston.

Wilmore, Jack (1976). Athletic Training and Physical Fitness: Physiological Principles of the Conditioning Process, Allyn and Bacon, Inc., Boston.

Examples

data(BodyFat)
head(BodyFat)

data-breastcancer

Gene expression signatures for p53 mutation status in 250 breast cancer samples

Description

Perturbations of the p53 pathway are associated with more aggressive and therapeutically refractory tumours. We preprocessed the data using Robust Multichip Analysis (RMA). Dataset has been truncated to the 1000 most informative genes (as selected by Wilcoxon test statistics) to simplify computation. The genes have been standardised to have zero mean and unit variance (i.e. z-scored).

Usage

data(breastcancer)

Format

A data frame with 250 observations on 1001 variables. The first 1000 columns are numerical variables; the last column (named code) is a factor with levels case and control.

Details

The factor code defines whether there was a mutation in the p53 sequence (code=case) or not (code=control).

Source

Dr. Chris Holmes, c.holmes at stats dot. ox . ac .uk

data-carcass 25

References

```
Miller et al (2005, PubMed ID:16141321)
```

Examples

```
data(breastcancer)
## maybe str(breastcancer); plot(breastcancer) ...
```

data-carcass

Lean meat contents of 344 pig carcasses

Description

Measurement of lean meat percentage of 344 pig carcasses together with auxillary information collected at three Danish slaughter houses

Usage

```
data(carcass)
```

Format

carcassall: A data frame with 344 observations on the following 17 variables.

weight Weight of carcass

lengthc Length of carcass from back toe to head (when the carcass hangs in the back legs)

lengthf Length of carcass from back toe to front leg (that is, to the shoulder)

lengthp Length of carcass from back toe to the pelvic bone

Fat02, Fat03, Fat11, Fat12, Fat13, Fat14, Fat16 Thickness of fat layer at different locations on the back of the carcass (FatXX refers to thickness at (or rather next to) rib no. XX. Notice that 02 is closest to the head

Meat11, Meat12, Meat13 Thickness of meat layer at different locations on the back of the carcass, see description above

LeanMeat Lean meat percentage determined by dissection

slhouse Slaughter house; a factor with levels a b c

sex Sex of the pig; a factor with a b c. Notice that it is no an error to have three levels; the third level refers to castrates

Note

carcass: Contains only the variables Fat11, Fat12, Fat13, Meat11, Meat12, Meat13, LeanMeat

26 data-chestSim

Source

Busk, H., Olsen, E. V., Brøndum, J. (1999) Determination of lean meat in pig carcasses with the Autofom classification system, Meat Science, 52, 307-314

Examples

```
data(carcass)
head(carcass)
```

data-chestSim

Simulated data from the Chest Clinic example

Description

Simulated data from the Chest Clinic example (also known as the Asia example) from Lauritzen and Spiegelhalter, 1988 (see reference below).

Usage

```
data(chestSim500)
```

Format

A data frame with 500 observations on the following 8 variables.

```
asia Recent visit to Asia?; a factor with levels yes no tub Has tuberculosis?; a factor with levels yes no
```

smoke Is a smoker?; a factor with levels yes no

lung Has lung cancer?; a factor with levels yes no

bronc Has bronchitis?; a factor with levels yes no

either Either lung cancer or tuberculosis?; a factor with levels yes no

xray Positive x-ray? a factor with levels yes no

dysp Dyspnoea (shortness of breath)?; a factor with levels yes no

Details

Notice that the chest clinic example is a contrieved example; it does not originate from an empirical study.

References

Lauritzen and Spiegelhalter (1988) Local Computations with Probabilities on Graphical Structures and their Application to Expert Systems (with Discussion). J. Roy. Stat. Soc. 50, p. 157-224.

data-dietox 27

Examples

```
data(chestSim500)
## maybe str(chestSim500) ; plot(chestSim500) ...
```

data-dietox

Growth curves of pigs in a 3x3 factorial experiment

Description

The dietox data frame has 861 rows and 7 columns.

Usage

data(dietox)

Format

This data frame contains the following columns: Weight, Feed, Time, Pig, Evit, Cu, Litter.

Source

Lauridsen, C., Højsgaard, S., Sørensen, M.T. C. (1999) Influence of Dietary Rapeseed Oli, Vitamin E, and Copper on Performance and Antioxidant and Oxidative Status of Pigs. J. Anim. Sci.77:906-916

Examples

data(dietox)

data-dumping

Gastric Dumping

Description

A contingency table relating surgical operation, centre and severity of gastric dumping, a syndrome associated with gastric surgery.

Usage

data(dumping)

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Format

A 3x4x4 table of counts cross-classified by Symptom (none/slight/moderate), Operation (Vd/Va/Vh/Gr) and Centre (1:4).

Details

Gastric dumping syndrome is a condition where ingested foods bypass the stomach too rapidly and enter the small intestine largely undigested. It is an undesirable side-effect of gastric surgery. The table summarizes the results of a study comparing four different surgical operations on patients with duodenal ulcer, carried out in four centres, as described in Grizzle et al (1969). The four operations were: vagotomy and drainage, vagotomy and antrectomy (removal of 25\ (removal of 50\) 75\

Source

Grizzle JE, Starmer CF, Koch GG (1969) Analysis of categorical data by linear models. Biometrics 25(3):489-504.

Examples

```
data(dumping)
plot(dumping)
```

data-lizard

Lizard behaviour

Description

In a study of lizard behaviour, characteristics of 409 lizards were recorded, namely species (S), perch diameter (D) and perch height (H). Perch means preferred place to settle down (a branch on a tree). The focus of interest is in how the propensities of the lizards to choose perch height and diameter are related, and whether and how these depend on species.

Usage

```
data(lizard)
```

Format

A 3-dimensional array with factors diam: "<=4" ">4" height: ">4.75" "<=4.75" species: "anoli" "dist"

References

Schoener TW (1968) The anolis lizards of bimini: Resource partitioning in a complex fauna. Ecology 49:704-726

data-mathmark 29

Examples

```
data(lizard)

# Datasets lizardRAW and lizardDF are generated with the following code
#lizardAGG <- as.data.frame(lizard)

#f <- lizardAGG$Freq
#idx <- unlist(mapply(function(i, n) rep(i, n), 1:8, f))
#set.seed(0805)
#idx <- sample(idx)
#lizardRAW <- as.data.frame(lizardAGG[idx, 1:3])
#rownames(lizardRAW) <- 1:NROW(lizardRAW)</pre>
```

data-mathmark

Mathematics marks for students

Description

The mathmark data frame has 88 rows and 5 columns.

Usage

```
data(mathmark)
```

Format

This data frame contains the following columns: mechanics, vectors, algebra, analysis, statistics.

Author(s)

```
Søren Højsgaard, <sorenh@math.aau.dk>
```

References

David Edwards, An Introduction to Graphical Modelling, Second Edition, Springer Verlag, 2000

```
data(mathmark)
```

30 data-milkcomp

data-mildew

Mildew fungus

Description

The data stem from a cross between two isolates of the barley powdery mildew fungus. For each offspring 6 binary characteristics, each corresponding to a single locus, were recorded. The object of the analysis is to determine the order of the loci along the chromosome.

Usage

```
data(mildew)
```

Format

A 6 dimensional array where each variable has levels "1" and "2". The variables are: 1a10, 1occ, mp58, c365, p53a and a365.

References

Christiansen, S.K., Giese, H (1991) Genetic analysis of obligate barley powdery mildew fungus based on RFLP and virulence loci. Theor. Appl. Genet. 79:705-712

Examples

```
data(mildew)
## maybe str(mildew) ; plot(mildew) ...
```

data-milkcomp

Milk composition data

Description

Data from an experiment on composition of sow milk. Milk composition is measured on four occasions during lactation on a number of sows. The treatments are different types of fat added to the sows feed.

Usage

```
data(milkcomp)
```

data-Nutrimouse 31

Format

A data frame with 214 observations on the following 7 variables.

```
sow a numeric vector
lactime a numeric vector
treat a factor with levels a b c d e f g
fat a numeric vector
protein a numeric vector
dm (dry matter) a numeric vector
lactose a numeric vector
```

Details

```
a is the control, i.e. no fat has been added.
fat + protein + lactose almost add up to dm (dry matter)
```

References

Charlotte Lauridsen and Viggo Danielsen (2004): Lactational dietary fat levels and sources influence milk composition and performance of sows and their progeny Livestock Production Science 91 (2004) 95-105

Examples

```
data(milkcomp)
## maybe str(milk) ; plot(milk) ...
```

data-Nutrimouse

The Nutrimouse Dataset

Description

The data come from a study of the effects of five dietary regimens with different fatty acid compositions on liver lipids and hepatic gene expression in 40 mice.

Usage

```
data(Nutrimouse)
```

Format

A data frame with 40 observations on 143 variables of which two are factors and 141 are numeric.

```
genotype a factor with levels wt ppar
diet a factor with levels coc fish lin ref sun
```

32 data-personality

Details

The data come from a study of the effects of five dietary regimens with different fatty acid compositions on liver lipids and hepatic gene expression in wild-type and PPAR-alpha-deficient mice (Martin et al., 2007).

There were 5 replicates per genotype and diet combination.

There are two design variables: (i) genotype, a factor with two levels: wild-type (wt) and PPAR-alpha-deficient (ppar), and (ii) diet, a factor with five levels. The oils used for experimental diet preparation were: corn and colza oils (50/50) for a reference diet (ref); hydrogenated coconut oil for a saturated fatty acid diet (coc); sunflower oil for an Omega6 fatty acid-rich diet (sun); linseed oil for an Omega3-rich diet (lin); and corn/colza/enriched (43/43/14) fish oils (fish).

There are 141 response variables: (i) the log-expression levels of 120 genes measured in liver cells, and (ii) the concentrations (in percentages) of 21 hepatic fatty acids measured by gas chromatography.

Source

The data were provided by Pascal Martin from the Toxicology and Pharmacology Laboratory, National Institute for Agronomic Research, France.

References

Martin, P. G. P., Guillou, H., Lasserre, F., D'jean, S., Lan, A., Pascussi, J.-M., San Cristobal, M., Legrand, P., Besse, P. and Pineau, T. (2007). Novel aspects of PPARa-mediated regulation of lipid and xenobiotic metabolism revealed through a multrigenomic study. Hepatology 54, 767-777.

Examples

data(Nutrimouse)

data-personality

Personality traits

Description

The peronality dataframe has 240 rows and 32 columns

Usage

data(personality)

Format

This dataframe has recordings on the following 32 variables: distant, talkatv, carelss, hardwrk, anxious, agreebl, tense, kind, opposng, relaxed, disorgn, outgoin, approvn, shy, discipl, harsh, persevr, friendl, worryin, respnsi, contrar, sociabl, lazy, coopera, quiet, organiz, criticl, lax, laidbck, withdrw, givinup, easygon

data-rats 33

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

References

Origin unclear

Examples

```
data(personality)
str(personality)
```

data-rats

Weightloss of rats

Description

An artificial dataset. 24 rats (12 female, 12 male) have been randomized to use one of three drugs (products for loosing weight). The weightloss for each rat is noted after one and two weeks.

Usage

data(rats)

Format

A dataframe with 4 variables. Sex: "M" (male), "F" (female). Drug: "D1", "D2", "D3" (three types). W1 weightloss, week one. W2 weightloss, week 2.

References

Morrison, D.F. (1976). Multivariate Statistical Methods. McGraw-Hill, USA.

Edwards, D. (1995). Introduction to Graphical Modelling, Springer-Verlag. New York.

34 data-wine

data-reinis

Risk factors for coronary heart disease.

Description

Data collected at the beginning of a 15 year follow-up study of probable risk factors for coronary thrombosis. Data are from all men employed in a car factory.

Usage

data(reinis)

Format

A table with 6 discrete variables. A: smoking, B: strenous mental work, D: strenuous physical work, E: systolic blood pressure, F: ratio of lipoproteins, G: Family anamnesis of coronary heart disease.

References

Edwards and Havranek (1985): A fast procedure for model search in multidimensional contingency tables. Biometrika, 72: 339-351.

Reinis et al (1981): Prognostic significance of the risk profile in the prevention of coronary heart disease. Bratis. lek. Listy. 76: 137-150.

data-wine

Chemical composition of wine

Description

Using chemical analysis determine the origin of wines

Usage

data(wine)

Format

A data frame with 178 observations on the following 14 variables.

Cult a factor with levels v1 v2 v3: 3 different graph varieties

Alch Alcohol

Mlca Malic acid

Ash Ash

Aloa Alcalinity of ash

data_cad 35

```
Mgns Magnesium
Ttlp Total phenols
Flvn Flavanoids
Nnfp Nonflavanoid phenols
Prnt Proanthocyanins
Clri Color intensity
Hue Hue
Oodw OD280/OD315 of diluted wines
Prln Proline
```

Details

Data comes from the UCI Machine Learning Repository. The grape variety Cult is the class identifier.

Source

Frank, A. & Asuncion, A. (2010). UCI Machine Learning Repository https://archive.ics.uci.edu/ml/. Irvine, CA: University of California, School of Information and Computer Science.

References

```
See references at https://archive.ics.uci.edu/ml/datasets/Wine/
```

Examples

```
data(wine)
## maybe str(wine) ; plot(wine) ...
```

data_cad

Coronary artery disease data

Description

A cross classified table with observational data from a Danish heart clinic. The response variable is CAD (coronary artery disease, some times called heart attack).

Usage

```
data(cad1)
```

36 data_cad

Format

A data frame with 236 observations on the following 14 variables.

Sex Sex; a factor with levels Female Male

AngPec Angina pectoris (chest pain attacks); a factor with levels Atypical None Typical

AMI Acute myocardic infarct; a factor with levels Definite NotCertain

QWave A reading from an electrocardiogram; a factor with levels No Yes; Yes means pathological and is a sign of previous myocardial infarction.

QWavecode a factor with levels Nonusable Usable. An assessment of whether QWave is reliable.

STcode a factor with levels Nonusable Usable. An assessment of whether STchange is reliable.

STchange A reading from an electrocardiogram; a factor with levels No Yes. An STchange indicates a blockage of the coronary artery.

SuffHeartF Sufficient heart frequency; a factor with levels No, Yes

Hypertrophi a factor with levels No, Yes. Hypertrophy refers to an increased size of the heart muscle due to exercise.

Hyperchol a factor with levels No Yes. Hypercholesterolemia, also called high cholesterol, is the presence of high levels of cholesterol in the blood.

Smoker Is the patient a smoker; a factor with levels No, Yes.

Inherit Hereditary predispositions for CAD; a factor with levels No, Yes.

Heartfail Previous heart failures; a factor with levels No Yes

CAD Coronary Artery Disease; a factor with levels No Yes. CAD refers to a reduction of blood flow to the heart muscle (commonly known as a heart attack). The diagnosis made from biopsies.

Details

Notice that data are collected at a heart clinic, so data do not represent the population, but are conditional on patients having ended up at the clinic.

- cad1: Complete dataset, 236 cases.
- cad2: Incomplete dataset, 67 cases. Information on (some of) the variables 'Hyperchol', 'Smoker' and 'Inherit' is missing.

References

Hansen, J. F. (1980). The clinical diagnoisis of ichaeme heart disease du to coronary artery disease. Danish Medical Bulletin

Højsgaard, Søren and Thiesson, Bo (1995). BIFROST - Block recursive models Induced From Relevant knowledge, Observations and Statistical Techniques. Computational Statistics and Data Analysis, vol. 19, p. 155-175

```
data(cad1)
## maybe str(cad1) ; plot(cad1) ...
```

downstream-aliases 37

downstream-aliases	Downstream aliases
downstream-allases	Downstream aliases

Description

Downstream aliases for other graphical modelling packages. Will be deprecated in due course.

fastcombn

Generate All Combinations of n Elements Taken m at a Time

Description

Generate all combinations of the elements of x taken m at a time. If x is a positive integer, returns all combinations of the elements of seq(x) taken m at a time.

Usage

```
fastcombn(x, m, FUN = NULL, simplify = TRUE, ...)
combn_prim(x, m, simplify = TRUE)
```

Arguments

X	vector source for combinations, or integer n for $x \leftarrow seq(n)$.
m	number of elements to choose.
FUN	function to be applied to each combination; default 'NULL' means the identity, i.e., to return the combination (vector of length 'm').
simplify	logical indicating if the result should be simplified to a matrix; if FALSE, the function returns a list.
	Further arguments passed on to FUN.

Details

- Factors x are accepted.
- combn_prim is a simplified (but faster) version of the combn function. Does nok take the FUN argument.
- fastcombn is intended to be a faster version of the combn function.

Value

A matrix or a list.

Author(s)

Søren Højsgaard

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See Also

combn

Examples

```
x \leftarrow letters[1:5]; m \leftarrow 3
fastcombn(x, m)
combn(x, m)
combn_prim(x, m)
x \leftarrow letters[1:4]; m \leftarrow 3
fastcombn(x, m, simplify=FALSE)
combn(x, m, simplify=FALSE)
combn_prim(x, m, simplify=FALSE)
x <- 1:10; m <- 3
fastcombn(x, m, min)
combn(x, m, min)
x \leftarrow factor(letters[1:8]); m \leftarrow 5
if (require(microbenchmark)){
  microbenchmark(
    combn(x, m, simplify=FALSE),
    combn_prim(x, m, simplify=FALSE),
    fastcombn(x, m, simplify=FALSE),
    times=50
  )
}
```

gmwr_book

Functions from Graphical Modelling with R book

Description

Functions that must be retained to make code from gmwr-book work

Usage

```
as.adjMAT(object)
```

Arguments

object

An object to be coerced.

graph-clique 39

Get cliques of an undirected graph

Description

Return a list of (maximal) cliques of an undirected graph.

Usage

```
get_cliques(object)
max_cliqueMAT(amat)
getCliques(object)
maxCliqueMAT(amat)
maxClique(object)
```

Arguments

object An undirected graph represented either as a graphNEL object, an igraph object,

a (dense) matrix, a (sparse) dgCMatrix

amat An adjacency matrix.

Details

In graph theory, a clique is often a complete subset of a graph. A maximal clique is a clique which can not be enlarged. In statistics (and that is the convention we follow here) a clique is usually understood to be a maximal clique.

Finding the cliques of a general graph is an NP complete problem. Finding the cliques of triangualted graph is linear in the number of cliques.

The workhorse is the max_cliqueMAT function which calls the maxClique function in the RBGL package.

Value

A list.

Synonymous functions

For backward compatibility with downstream packages we have the following synonymous functions:

- getCliques = get_cliques
- maxCliqueMAT = max_cliqueMAT

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Author(s)

```
Søren Højsgaard, <sorenh@math.aau.dk>
```

See Also

```
ug, dag, mcs, mcsMAT, rip, ripMAT, moralize, moralizeMAT
```

Examples

```
## graphNEL
uG0 <- ug(~a:b + b:c + c:d + d:e + e:f + f:a) # a graphNEL object
get_cliques(uG0)

uG1 <- as(uG0, "igraph")
get_cliques(uG1)

uG2 <- as(uG0, "matrix")
get_cliques(uG2)

uG3 <- as(uG1, "dgCMatrix")
get_cliques(uG3)</pre>
```

graph-coerce

Graph coercion

Description

Methods for changing graph representations

Usage

```
coerceGraph(object, class)
graph_as(object, outtype, intype = NULL)
```

Arguments

is a list)

Details

coerceGraph is used in the book "Graphical models with R". A more generic approach is as().

graph-coerce-api 41

Examples

```
g1 <- ug(~a:b+b:c)
as(g1, "igraph")
as(g1, "matrix")
as(g1, "Matrix")
as(g1, "dgCMatrix")

## graph_as(g1, "ugList") ## Fails
## getCliques(g1) ## Works

11 <- list(c("a" ,"b"), c("b", "c"))
graph_as(11, "graphNEL", "ugList")</pre>
```

graph-coerce-api

API for coercing graph representations

Description

API for coercing graph representations.

Usage

```
g_dm2sm_(object)
g_dm2ig_(object)
g_sm2dm_(object)
g_sm2ig_(object)
g_ig2dm_(object)
g_ig2sm_(object)
g_xm2ig_(object)
g_xm2dm_(object)
g_xm2dm_(object)
g_xm2xm_(object)
```

Arguments

object An object representing a graph
result Either 'matrix' (dense) or 'dgCMatrix' (sparse, can be abbreviated to 'Matrix').

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Details

No checking is made. In the function the following names are used:

```
"ig": "igraph";"gn": "graphNEL";"sm": "dgCMatrix" (sparse matrix);"dm": "matrix" (dense matrix)
```

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
ug, dag
```

graph-create

Create undirected and directed graphs

Description

These functions are wrappers for creation of graphs as implemented by graphNEL objects in the graph package.

Usage

```
ug(..., result = "igraph")
ugi(...)

ugList(x, result = "igraph")

dag(..., result = "igraph", forceCheck = FALSE)

dagi(..., forceCheck = FALSE)

dagList(x, result = "igraph", forceCheck = FALSE)
```

Arguments

... A generating class for a graph, see examples below

The format of the graph. The possible choices are "graphNEL" (for a graphNEL object), "igraph" (for an igraph object), "matrix" (for an adjacency matrix), "dgCMatrix" (for a sparse matrix).

X A list or individual components from which a graph can be created.

ForceCheck Logical determining if it should be checked if the graph is acyclical. Yes, one can specify graphs with cycles using the dag() function.

graph-edgeList 43

Value

Functions ug(), and dag() can return a graphNEL object, an igraph object, a sparse or a dense adjacency matrix.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
## The following specifications of undirected graphs are equivalent:
uG1 \leftarrow ug(\sim a:b:c + c:d)
uG2 <- ug(c("a", "b", "c"), c("c", "d"))
uG3 \leftarrow ug(c("a", "b"), c("a", "c"), c("b", "c"), c("c", "d"))
## The following specifications of directed acyclig graphs are equivalent:
daG1 \leftarrow dag(\sim a:b:c + b:c + c:d)
daG2 <- dag(c("a", "b", "c"), c("b", "c"), c("c", "d"))
## dag() allows to specify directed graphs with cycles:
daG4 <- dag(~ a:b + b:c + c:a) # A directed graph but with cycles
## A check for acyclicity can be done with
## daG5 <- dag(\sim a:b + b:c + c:a, forceCheck=TRUE)
## A check for acyclicity is provided by topoSort
topo_sort( daG2 )
topo_sort( daG4 )
## Different representations
uG7 <- ug(~a:b:c + c:d, result="igraph")
                                              # igraph
uG8 <- ug(~a:b:c + c:d, result="matrix")
                                             # dense matrix
uG9 <- ug(~a:b:c + c:d, result="dgCMatrix") # sparse matrix
```

graph-edgeList

Find edges in a graph and edges not in a graph.

Description

Returns the edges of a graph (or edges not in a graph) where the graph can be either a graphNEL object, an igraph object or an adjacency matrix.

Usage

```
edgeList(object, matrix = FALSE)
edgeListMAT(adjmat, matrix = FALSE)
```

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```
nonEdgeList(object, matrix = FALSE)
nonEdgeListMAT(adjmat, matrix = FALSE)
```

Arguments

object A graphNEL object, an igraph object, a dense matrix or a sparse dgCMatrix

(the two latter representing an adjacency matrix).

matrix If TRUE the result is a matrix; otherwise the result is a list.

adjmat An adjacency matrix.

Examples

```
## A graph with edges
g \leftarrow ug(a:b + b:c + c:d)
gm <- as(g, "matrix")</pre>
edgeList(g)
edgeList(gm)
edgeListMAT(gm)
edgeList(g, matrix=TRUE)
edgeList(gm, matrix=TRUE)
edgeListMAT(gm, matrix=TRUE)
nonEdgeList(g)
nonEdgeList(gm)
nonEdgeListMAT(gm)
## A graph without edges
g \leftarrow ug(a + b + c)
gm <- as(g, "matrix")</pre>
edgeList(g)
edgeList(gm)
edgeListMAT(gm)
edgeList(g, matrix=TRUE)
edgeList(gm, matrix=TRUE)
edgeListMAT(gm, matrix=TRUE)
nonEdgeList(g)
nonEdgeList(gm)
nonEdgeListMAT(gm)
```

graph-gcproperties

Properties of a generating class (for defining a graph).

Description

A set of generators define an undirected graph, here called a dependence graph. Given a set of generators it is checked 1) if the dependence dependence graph is in 1-1-correspondance with the genrators (such that the corresponding model is graphical) and 2) if the dependence graph is chordal (triangulated) (such that the corresponding model is decomposable).

graph-gcproperties 45

Usage

```
isGraphical(x)
isDecomposable(x)
```

Arguments

x A generating class given as right hand sided formula or a list; see examples below.

Details

A set of sets of variables, say A_1, A_2, ... A_K is called a generating class for a graph with vertices V and edges E. If two variables a,b are in the same generator, say A_j, then a and b are vertices in the graph and there is an undirected edge between a and b.

```
The graph induced by code\{g1 = a:b + a:c + b:c + c:d\} has edges code\{ab, ac, bc, cd\}. The cliques of this graph are code\{abc, cd\}. Hence there is not a 1-1-correspondance between the graph and the generators.
```

On the other hand, $\code{g2 \leftarrow \capacite{g2 \leftarrow \capacite{g2 \leftarrow \cap{g2 \leftarrow \cap$

The graph induced by $\code{g3 <- ~a:b + b:c + c:d + d:a}$ is in 1-1-correspondance with its dependence graph, but the graph is not chordal.

Value

TRUE or FALSE

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
mcs, rip
```

Examples

```
g1 <- ~a:b + a:c + b:c + c:d
g2 <- ~a:b:c + c:d
g3 <- ~a:b + b:c + c:d + d:a

isGraphical( g1 ) # FALSE
isGraphical( g2 ) # TRUE
isGraphical( g3 ) # TRUE</pre>
```

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```
isDecomposable( g1 ) # FALSE
isDecomposable( g2 ) # TRUE
isDecomposable( g3 ) # TRUE

## A generating class can be given as a list:
f <- list(c("a","b"), c("b","c"), c("a","c"))
isGraphical( f )
isDecomposable( f )</pre>
```

graph-mcs

Maximum cardinality search on undirected graph.

Description

Returns (if it exists) a perfect ordering of the vertices in an undirected graph.

Usage

```
mcs(object, root = NULL, index = FALSE)

## Default S3 method:
mcs(object, root = NULL, index = FALSE)

mcsMAT(amat, vn = colnames(amat), root = NULL, index = FALSE)

mcs_marked(object, discrete = NULL, index = FALSE)

## Default S3 method:
mcs_marked(object, discrete = NULL, index = FALSE)

mcs_marked(object, discrete = NULL, index = FALSE)

mcs_markedMAT(amat, vn = colnames(amat), discrete = NULL, index = FALSE)
```

Arguments

object An undirected graph represented either as a graphNEL object, an igraph, a

(dense) matrix, a (sparse) dgCMatrix.

root A vector of variables. The first variable in the perfect ordering will be the first

variable on 'root'. The ordering of the variables given in 'root' will be followed

as far as possible.

index If TRUE, then a permutation is returned

amat Adjacency matrix

vn Nodes in the graph given by adjacency matrix

discrete A vector indicating which of the nodes are discrete. See 'details' for more infor-

mation.

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Details

An undirected graph is decomposable iff there exists a perfect ordering of the vertices. The maximum cardinality search algorithm returns a perfect ordering of the vertices if it exists and hence this algorithm provides a check for decomposability. The mcs() functions finds such an ordering if it exists.

The notion of strong decomposability is used in connection with e.g. mixed interaction models where some vertices represent discrete variables and some represent continuous variables. Such graphs are said to be marked. The \code{mcsmarked()} function will return a perfect ordering iff the graph is strongly decomposable. As graphs do not know about whether vertices represent discrete or continuous variables, this information is supplied in the \code{discrete} argument.

Value

A vector with a linear ordering (obtained by maximum cardinality search) of the variables or character(0) if such an ordering can not be created.

Note

The workhorse is the mcsMAT function.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
moralize, junction_tree, rip, ug, dag
```

Examples

```
uG <- ug(~ me:ve + me:al + ve:al + al:an + al:st + an:st)
mcs(uG)
mcsMAT(as(uG, "matrix"))
## Same as
uG <- ug(~ me:ve + me:al + ve:al + al:an + al:st + an:st, result="matrix")
mcsMAT(uG)

## Marked graphs
uG1 <- ug(~ a:b + b:c + c:d)
uG2 <- ug(~ a:b + a:d + c:d)
## Not strongly decomposable:
mcs_marked(uG1, discrete=c("a","d"))
## Strongly decomposable:
mcs_marked(uG2, discrete=c("a","d"))</pre>
```

graph-min-triangulate Minimal triangulation of an undirected graph

Description

An undirected graph uG is triangulated (or chordal) if it has no cycles of length >= 4 without a chord which is equivalent to that the vertices can be given a perfect ordering. Any undirected graph can be triangulated by adding edges to the graph, so called fill-ins which gives the graph TuG. A triangulation TuG is minimal if no fill-ins can be removed without breaking the property that TuG is triangulated.

Usage

```
minimal_triang(
  object,
  tobject = triangulate(object),
  result = NULL,
  details = 0
)
minimal_triangMAT(amat, tamat = triangulateMAT(amat), details = 0)
```

Arguments

object	An undirected graph represented either as a graphNEL object, a (dense) matrix, a (sparse) dgCMatrix.
tobject	Any triangulation of object; must be of the same representation.
result	The type (representation) of the result. Possible values are "graphNEL", "matrix", "dgCMatrix". Default is the same as the type of object.
details	The amount of details to be printed.
amat	The undirected graph which is to be triangulated; a symmetric adjacency matrix.
tamat	Any triangulation of object; a symmetric adjacency matrix.

Details

For a given triangulation tobject it may be so that some of the fill-ins are superflous in the sense that they can be removed from tobject without breaking the property that tobject is triangulated. The graph obtained by doing so is a minimal triangulation.

```
Notice: A related concept is the minimum triangulation, which is the the graph with the smallest number of fill-ins. The minimum triangulation is unique. Finding the minimum triangulation is NP-hard.
```

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Value

minimal_triang() returns a graphNEL object while minimal_triangMAT() returns an adjacency matrix.

Author(s)

Clive Bowsher C.Bowsher@statslab.cam.ac.uk with modifications by Søren Højsgaard, <sorenh@math.aau.dk>

References

Kristian G. Olesen and Anders L. Madsen (2002): Maximal Prime Subgraph Decomposition of Bayesian Networks. IEEE TRANSACTIONS ON SYSTEMS, MAN AND CYBERNETICS, PART B: CYBERNETICS, VOL. 32, NO. 1, FEBRUARY 2002

See Also

```
mpd, rip, triangulate
```

Examples

```
## An igraph object
g1 <- ug(~a:b + b:c + c:d + d:e + e:f + a:f + b:e, result="igraph")
x <- minimal_triang(g1)

tt <- ug(~a:b:e:f + b:e:c:d, result="igraph")
x <- minimal_triang(g1, tobject=tt)

## g2 is a triangulation of g1 but it is not minimal
g2 <- ug(~a:b:e:f + b:c:d:e, result="igraph")
x <- minimal_triang(g1, tobject=g2)

## An adjacency matrix
g1m <- ug(~a:b + b:c + c:d + d:e + e:f + a:f + b:e, result="matrix")
x <- minimal_triangMAT(g1m)</pre>
```

graph-moralize

Moralize a directed acyclic graph

Description

Moralize a directed acyclic graph which means marrying parents and dropping directions.

Usage

```
moralize(object, ...)
## Default S3 method:
moralize(object, result = NULL, ...)
```

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Arguments

object	A directed acyclic graph represented either as a graphNEL object, an igraph, a (dense) matrix, a (sparse) dgCMatrix.
• • •	Additional arguments, currently not used
result	The representation of the moralized graph. When NULL the representation will be the same as the input object.

Value

A moralized graph represented either as a graphNEL, a dense matrix or a sparse dgCMatrix.

Note

The workhorse is the moralizeMAT function.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
mcs, junction_tree, rip, ug, dag
```

Examples

```
daG <- dag(~me+ve,~me+al,~ve+al,~al+an,~al+st,~an+st)
moralize(daG)

daG <- dag(~me+ve,~me+al,~ve+al,~al+an,~al+st,~an+st, result="matrix")
moralizeMAT(daG)

if (require(igraph)){
    M <- matrix(c(1,2,3,3), nrow=2)
    G <- graph.edgelist(M)
    G
    V(G)$name
moralize(G)
}</pre>
```

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graph-mpd	Maximal prime subgraph decomposition	

Description

Finding a junction tree representation of the MPD (maximal prime subgraph decomposition) of an undirected graph The maximal prime subgraph decomposition of a graph is the smallest subgraphs into which the graph can be decomposed.

Usage

```
mpd(object, tobject = minimal_triang(object), details = 0)
## Default S3 method:
mpd(object, tobject = triangulate(object), details = 0)
mpdMAT(amat, tamat = minimal_triangMAT(amat), details = 0)
```

Arguments

object	An undirected graph; a graphNEL object, an igraph or an adjacency matrix.
tobject	Any minimal triangulation of object; a graphNEL object, an igraph or an adjacency matrix.
details	The amount of details to be printed.
amat	An undirected graph; a symmetric adjacency matrix
tamat	Any minimal triangulation of object; a symmetric adjacency matrix

Value

A list with components "nodes", "cliques", "separators", "parents", "children", "nLevels". The component "cliques" defines the subgraphs.

Author(s)

Clive Bowsher < C. Bowsher@statslab.cam.ac.uk> with modifications by Søren Højsgaard, < sorenh@math.aau.dk>

References

Kristian G. Olesen and Anders L. Madsen (2002): Maximal Prime Subgraph Decomposition of Bayesian Networks. IEEE TRANSACTIONS ON SYSTEMS, MAN AND CYBERNETICS, PART B: CYBERNETICS, VOL. 32, NO. 1, FEBRUARY 2002

See Also

mcs, mcsMAT, minimal_triang, minimal_triangMAT, rip, ripMAT, triangulate, triangulateMAT

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Examples

```
## Maximal prime subgraph decomposition - a graphNEL object
g1 <- ug(~ a:b + b:c + c:d + d:e + e:f + a:f + b:e)
if (interactive()) plot(g1)
x <- mpd(g1)

## Maximal prime subgraph decomposition - an adjacency matrix
g1m <- ug(~ a:b + b:c + c:d + d:e + e:f + a:f + b:e, result="matrix")
if (interactive()) plot(as(g1m, "graphNEL"))
x <- mpdMAT(g1m)</pre>
```

graph-randomdag

Random directed acyclic graph

Description

Generate a random directed acyclic graph (DAG)

Usage

```
random_dag(V, maxpar = 3, wgt = 0.1)
```

Arguments

V The set of vertices.

maxpar The maximum number of parents each node can have

wgt A parameter controlling how likely it is for a node to have a certain number of

parents; see 'Details'.

Details

If the maximum number of parents for a node is, say 3 and wgt=0.1, then the probability of the node ending up with 0,1,2,3 parents is proportional to 0.1^o0, 0.1^o1, 0.1^o2, 0.1^o3.

Value

A graphNEL object.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

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Examples

```
dg <- random_dag(1:1000, maxpar=5, wgt=.9)
table(sapply(vpar(dg),length))

dg <- random_dag(1:1000, maxpar=5, wgt=.5)
table(sapply(vpar(dg),length))

dg <- random_dag(1:1000, maxpar=5, wgt=.1)
table(sapply(vpar(dg),length))</pre>
```

graph-rip

Create RIP ordering of the cliques of an undirected graph; create junction tree.

Description

A RIP (running intersection property) ordering of the cliques is also called a perfect ordering. If the graph is not chordal, then no such ordering exists.

Usage

```
rip(object, ...)
## Default S3 method:
rip(object, root = NULL, nLevels = NULL, ...)

ripMAT(amat, root = NULL, nLevels = rep(2, ncol(amat)))
junction_tree(object, ...)

## Default S3 method:
junction_tree(object, nLevels = NULL, ...)

junction_treeMAT(amat, nLevels = rep(2, ncol(amat)), ...)

jTree(object, ...)
```

Arguments

object An undirected graph represented either as a graphNEL object, an igraph, a (dense) matrix, a (sparse) dgCMatrix.

.. Additional arguments; currently not used

root A vector of variables. The first variable in the perfect ordering will be the first

variable on 'root'. The ordering of the variables given in 'root' will be followed

as far as possible.

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nLevels Typically, the number of levels of the variables (nodes) when these are discrete.

Used in determining the triangulation using a "minimum clique weight heuris-

tic". See section 'details'.

amat Adjacency matrix

Details

The RIP ordering of the cliques of a decomposable (i.e. chordal) graph is obtained by first ordering the variables linearly with maximum cardinality search (by mcs). The root argument is transferred to mcs as a way of controlling which clique will be the first in the RIP ordering. The junction_tree() (and junction_tree()) (for "junction tree") is just a wrapper for a call of triangulate() followed by a call of rip().

Value

rip returns a list (an object of class ripOrder. A print method exists for such objects.)

Synonymous functions

For backward compatibility with downstream packages we have the following synonymous functions:

- jTree = junction_tree (Used in rags2ridges)
- junctionTree = junction_tree

Note

The workhorse is the ripMAT() function. The nLevels argument to the rip functions has no meaning.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
mcs, triangulate, moralize, ug, dag
```

Examples

```
## graphNEL
uG <- ug(~me:ve + me:al + ve:al + al:an + al:st + an:st)
mcs(uG)
rip(uG)
junction_tree(uG)

## Adjacency matrix
uG <- ug(~me:ve:al + al:an:st, result="matrix")
mcs(uG)
rip(uG)</pre>
```

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```
junction_tree(uG)

## Sparse adjacency matrix
uG <- ug(c("me", "ve", "al"), c("al", "an", "st"), result="dgCMatrix")
mcs(uG)
rip(uG)
junction_tree(uG)

## Non--decomposable graph
uG <- ug(~1:2 + 2:3 + 3:4 + 4:5 + 5:1)
mcs(uG)
rip(uG)
junction_tree(uG)</pre>
```

graph-triangulate

Triangulation of an undirected graph

Description

This function will triangulate an undirected graph by adding fill-ins.

Usage

```
triangulate(object, ...)
## Default S3 method:
triangulate(object, nLevels = NULL, result = NULL, check = TRUE, ...)
triang_mcwh(object, ...)

triang_elo(object, ...)

## Default S3 method:
triang(object, control = list(), ...)

## Default S3 method:
triang_mcwh(object, nLevels = NULL, result = NULL, check = TRUE, ...)

## Default S3 method:
triang_mcwh(object, nLevels = NULL, result = NULL, check = TRUE, ...)

## Default S3 method:
triang_elo(object, order = NULL, result = NULL, check = TRUE, ...)

triangulateMAT(amat, nLevels = rep(2, ncol(amat)), ...)

triang_mcwhMAT_(amat, nLevels = rep(2, ncol(amat)), ...)
```

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```
triang_eloMAT_(amat, order)
triang_eloMAT(amat, order = NULL)
```

Arguments

object An undirected graph represented either as a graphNEL object, an igraph, a (dense) matrix, a (sparse) dgCMatrix. Additional arguments, currently not used. . . . nLevels The number of levels of the variables (nodes) when these are discrete. Used in determining the triangulation using a "minimum clique weight heuristic". See section 'details'. The type (representation) of the result. Possible values are "graphNEL", "igraph", result "matrix", "dgCMatrix". Default is the same as the type of object. If TRUE (the default) it is checked whether the graph is triangulated before doing check the triangulation; gives a speed up if FALSE control A list controlling the triangulation; see 'examples'. order Elimation order; a character vector or numeric vector.

Adjacency matrix; a (dense) matrix, or a (sparse) dgCMatrix.

Details

amat

There are two type of functions: triang and triangulate

The workhorse is the triangulateMAT function.

The triangulation is made so as the total state space is kept low by applying a minimum clique weight heuristic: When a fill-in is necessary, the algorithm will search for an edge to add such that the complete set to be formed will have as small a state-space as possible. It is in this connection that the nLevels values are used.

Default (when nLevels=NULL) is to take nLevels=2 for all nodes. If nLevels is the same for all nodes then the heuristic aims at keeping the clique sizes small.

Value

A triangulated graph represented either as a graphNEL, a (dense) matrix or a (sparse) dgCMatrix.

Note

Care should be taken when specifying nLevels for other representations than adjacency matrices: Since the triangulateMAT function is the workhorse, any other representation is transformed to an adjacency matrix and the order of values in nLevels most come in the order of the nodes in the adjacency matrix representation.

Currently there is no check for that the graph is undirected.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

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See Also

```
ug, dag, mcs, mcsMAT, rip, ripMAT, moralize, moralizeMAT
```

Examples

```
## graphNEL
uG1 \leftarrow ug(a:b + b:c + c:d + d:e + e:f + f:a)
uG2 \leftarrow ug(a:b + b:c + c:d + d:e + e:f + f:a, result="matrix")
uG3 <- ug(~a:b + b:c + c:d + d:e + e:f + f:a, result="dgCMatrix")
## Default triangulation: minimum clique weight heuristic
# (default is that each node is given the same weight):
tuG1 <- triang(uG1)</pre>
## Same as
triang_mcwh(uG1)
## Alternative: Triangulation from a desired elimination order
# (default is that the order is order of the nodes in the graph):
triang(uG1, control=list(method="elo"))
## Same as:
triang_elo(uG1)
## More control: Define the number of levels for each node:
tuG1 <- triang(uG1, control=list(method="mcwh", nLevels=c(2, 3, 2, 6, 4, 9)))
tuG1 <- triang_mcwh(uG1, nLevels=c(2, 3, 2, 6, 4, 9))
tuG1 <- triang(uG1, control=list(method="elo", order=c("a", "e", "f")))</pre>
tuG1 <- triang_elo(uG1, order=c("a", "e", "f"))</pre>
## graphNEL
uG1 \leftarrow ug(a:b + b:c + c:d + d:e + e:f + f:a)
tuG1 <- triangulate(uG1)</pre>
## adjacency matrix
uG2 <- ug(~a:b + b:c + c:d + d:e + e:f + f:a, result="matrix")
tuG2 <- triangulate(uG2)</pre>
## adjacency matrix (sparse)
uG2 <- ug(~a:b + b:c + c:d + d:e + e:f + f:a, result="dgCMatrix")
tuG2 <- triangulate(uG2)</pre>
```

graph_coerce_list

Coercion of graphs represented as lists

Description

Coercion of graphs represented as lists to various graph formats.

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Usage

```
g_ugl2ig_(zz, vn = NULL)
g_ugl2dm_(zz, vn = NULL)
g_ugl2sm_(zz, vn = NULL)
g_ugl2XX_(zz, outtype, vn = NULL)
g_dagl2ig_z, vn = NULL
g_dag12dm_(zz, vn = NULL)
g_dagl2sm_(zz, vn = NULL)
g_dagl2XX_(zz, outtype, vn = NULL)
g_adl2ig_(zz)
g_adl2dm_(zz)
g_adl2sm_(zz)
g_adl2XX_(zz, outtype)
g_M2adl_(amat)
g_M2ugl_(amat)
g_M2dagl_(amat)
g_ugl2M_(glist, vn = NULL, result = "matrix")
g_dagl2M_(glist, vn = NULL, result = "matrix")
g_adl2M_(alist, result = "matrix")
```

Arguments zz

vn	The names of the vertices in the graphs.	These will be the row and column
*	The names of the vertices in the graphs.	These will be the low and column

names of the matrix.

outtype What should a list be coerced to.

amat Adjacency matrix (dense or sparse dgCMatrix).

An object representing a graph.

glist A list of generators where a generator is a character vector. If interpreted as generators of an undirected graph, a generator is a complete set of vertices in

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the graph. If interpreted as generators of a dag, a generator (v1,...,vn) means that there will be arrows from v2,...,vn to v1.

result A graph object.
alist An adjacency list.

Examples

```
## Sparse and dense adjacency matrices converted to adjacency list
g1 <- ug(~a:b + b:c + c:d, result="matrix")
g2 <- ug(~a:b + b:c + c:d, result="dgCMatrix")
g_M2adl_( g1 )

## Sparse and dense adjacency matrices converted to cliques
g_M2ugl_( g1 )

## Sparse and dense adjacency matrices converted to cliques
g_M2dagl_( g1 )

## g_M2adl_( g2 ) ## FIXME FAILS for sparse matrix
## g_M2ugl_( g2 ) ## FIXME Is there an issue here??
## g_M2dagList( g2 ) ## Fails for sparse matrix</pre>
```

graph_iplot

Function for plotting graphs using the 'igraph' package.

Description

Generic function for plotting graphs using the 'igraph' package and a plot method for graphNEL objects.

Usage

```
iplot(x, ...)
## S3 method for class 'igraph'
iplot(x, ...)
```

Arguments

x A graph object to be plotted.... Additional arguments

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

graph_is

Examples

```
UG <- ug(~a:b+b:c:d)
iplot(UG)</pre>
```

graph_is

Check properties of graphs.

Description

Check if a graph is 1) a directed acyclic graph (DAG), 2) a directed graph (DG), 3) an undirected graph (UG), 4) a triangulated (chordal) undirected graph (TUG).

Usage

```
is_dag(object)
is_dagMAT(object)
is_ug(object)
is_ugMAT(object)
is_tug(object)
is_tugMAT(object)
is_dg(object)
is_dgMAT(object)
is_adjMAT(object)
is_adjMAT(object)
is_adjMAT(object)
```

Arguments

object

A graph represented as a graphNEL (graph package), an igraph (igraph package), an adjacency matrix or a sparse adjacency matrix (a dgCMatrix from the Matrix package).

Details

• A non-zero value at entry (i,j) in an adjacency matrix A for a graph means that there is an edge from i to j. If also (j,i) is non-zero there is also an edge from j to i. In this case we may think of a bidirected edge between i and j or we may think of the edge as being undirected.

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We do not distinguish between undirected and bidirected edges in the gRbase package. On the other hand, graphNEL objects from the graph package makes such a distinction (the function edgemode() will tell if edges are "directed" or "undirected" in a graphNEL object).

- The function is_ug() checks if the adjacency matrix is symmetric (If applied to a graphNEL, the adjacency matrix is created and checked for symmetry.)
- The function is_tug() checks if the graph is undirected and triangulated (also called chordal) by checking if the adjacency matrix is symmetric and the vertices can be given a perfect ordering using maximum cardinality seach.
- The function is_dg() checks if a graph is directed, i.e., that there are no undirected edges. This is done by computing the elementwise product of A and the transpose of A; if there are no non-zero entries in this product then the graph is directed.
- The function is_dag() will return TRUE if all edges are directed and if there are no cycles in the graph. (This is checked by checking if the vertices in the graph can be given a topological ordering which is based on identifying an undirected edge with a bidrected edge).
- There is a special case, namely if the graph has no edges at all (such that the adjacency matrix consists only of zeros). Such a graph is both undirected, triangulated, directed and directed acyclic.

Synonymous functions

The functions

• is.TUG/is.DAG/is.DG/is.UG/is.adjMAT

are synonymous with

• is_tug/is_dag/is_dg/is_ug/is_adjMAT.

The is. X group of functions will be deprecated.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

See Also

```
dag, ug
```

Examples

```
## DAGs
dag_ <- dag(~ a:b:c + c:d:e)
## Undirected graphs
ug_ <- ug(~a:b:c + c:d:e)
## Is graph a DAG?
is_dag(dag_)
is_dag(ug_)</pre>
```

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```
## Is graph an undirected graph
is_ug(dag_)
is_ug(ug_)

## Is graph a triangulated (i.e. chordal) undirected graph
is_tug(dag_)
is_tug(ug_)

## Example where the graph is not triangulated
ug2_ <- ug(~ a:b + b:c + c:d + d:a)
is_tug(ug2_)</pre>
```

graph_query

Query a graph

Description

Unified approach to query a graph about its properties (based partly on functionality from gRbase and functionality imported from RBGL).

Usage

```
querygraph(object, op, set = NULL, set2 = NULL, set3 = NULL)
qgraph(object, op, set = NULL, set2 = NULL, set3 = NULL)
ancestors(set, object)
subGraph(set, object)
is.triangulated(object)
connComp(object)
ancestralSet(set, object)
ancestralGraph(set, object)
parents(set, object)
children(set, object)
separates(set, set2, set3, object)
closure(set, object)
```

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```
adj(object, set)
is.simplicial(set, object)
simplicialNodes(object)
is.complete(object, set = NULL)
is.decomposition(set, set2, set3, object)
nodes_(object)
nodes(object, ...)
## S4 method for signature 'igraph'
nodes(object, ...)
edges(object)
edges_(object)
addEdge(v1, v2, object)
removeEdge(v1, v2, object)
```

Arguments

object A graph.

op The operation or query.

set, set2, set3 Sets of nodes in graph.

... additional arguments

v1, v2 Vertex names

Examples

```
ug0 <- ug(~a:b + b:c:d + e)
separates("a", "d", c("b", "c"), ug0)
separates("a", "d", "c", ug0)
is.simplicial("b", ug0)
simplicialNodes(ug0)
simplicialNodes(ug0)</pre>
```

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graph_topo_sort	Topological sort of vertices in directed acyclic graph	

Description

A topological ordering of a directed graph is a linear ordering of its vertices such that, for every edge (u->v), u comes before v in the ordering. A topological ordering is possible if and only if the graph has no directed cycles, that is, if it is a directed acyclic graph (DAG). Any DAG has at least one topological ordering. Can hence be used for checking if a graph is a DAG.

Usage

```
topo_sort(object, index = FALSE)
topo_sortMAT(amat, index = FALSE)
topoSort(object, index = FALSE)
topoSortMAT(amat, index = FALSE)
```

Arguments

object An graph represented either as a graphNEL object, an igraph, a (dense) matrix,

a (sparse) dgCMatrix.

index If FALSE, an ordering is returned if it exists and character(0) otherwise. If

TRUE, the index of the variables in an adjacency matrix is returned and -1

otherwise.

amat Adjacency matrix.

Value

If FALSE, an ordering is returned if it exists and character(0) otherwise. If TRUE, the index of the variables in an adjacency matrix is returned and -1 otherwise.

Synonymous functions

The functions topo_sort / topoSort are synonymous with topo_sortMAT / topoSortMAT. One of the groups may be deprecated in the future.

Note

The workhorse is the topo_sortMAT function which takes an adjacency matrix as input.

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

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See Also

```
dag, ug
```

Examples

```
dagMAT <- dag(~a:b:c + c:d:e, result="matrix")
dagMATS <- as(dagMAT, "dgCMatrix")

topo_sort(dagMAT)
topo_sort(dagMATS)</pre>
```

graph_vpar

List of vertices and their parents for graph.

Description

Get list of vertices and their parents for graph.

Usage

```
vchi(object, getv = TRUE, forceCheck = TRUE)
vchiMAT(object, getv = TRUE, forceCheck = TRUE)
vpar(object, getv = TRUE, forceCheck = TRUE)
vparMAT(object, getv = TRUE, forceCheck = TRUE)
```

Arguments

object An object representing a graph. Valid objects are an adjacency matrix or as a

graphNEL.

getv The result is by default a list of vectors of the form (v, pa1, pa2, ... paN)

where pa1, pa2, ... paN are the parents of v. If getv is FALSE then the vectors

will have the form (pa1, pa2, ... paN)

forceCheck Logical indicating if it should be checked that the object is a DAG.

Value

A list of vectors where each vector will have the form (v, pa1, pa2, ..., paN) where pa1, pa2, ... paN are the parents of v.

See Also

dag, ug

66 gRbase

Examples

```
## DAGs
dag_mat <- dag(~a:b:c + c:d:e, result="matrix")</pre>
dag_ig \leftarrow dag(\sim a:b:c + c:d:e)
vpar(dag_mat)
vpar(dag_ig)
vpar(dag_mat, getv=FALSE)
vpar(dag_ig, getv=FALSE)
## Undirected graphs
ug_mat <- ug(~a:b:c + c:d:e, result="matrix")</pre>
ug_ig \leftarrow ug(a:b:c + c:d:e)
## Not run:
## This will fail because the adjacency matrix is symmetric and the
## graphNEL has undirected edges
vpar(ug_mat)
vpar(ug_ig)
## End(Not run)
## When forceCheck is FALSE, it will not be detected that the
#g raphs are undirected.
vpar(ug_mat, forceCheck=FALSE)
vpar(ug_ig, forceCheck=FALSE)
```

gRbase

The package 'gRbase': summary information

Description

This package provides a basis for graphical modelling in R and in particular for other graphical modelling packages, most notably **gRim**, **gRain** and **gRc**.

Details

gRbase provides the following:

- Implementation of various graph algorithms, including maximum cardinality search, maximal prime subgraph decomposition, triangulation. See the vignette graphs.
- Implementation of various "high level" array operations, including multiplication/division, marginalization, slicing, permutation. See the vignette ArrayOps.
- Implementation of various "low level" array operations. See the vignette ArrayOpsPrim.
- A collection of datasets
- A general framework for setting up data and model structures and provide examples for fitting hierarchical log linear models for contingency tables and graphical Gaussian models for the multivariate normal distribution. (Notice: This last part is not maintained / developed further.)

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Authors

Soren Hojsgaard, Department of Mathematical Sciences, Aalborg University, Denmark Contributions from Claus Dethlefsen, Clive Bowsher, David Edwards.

Acknowledgements

Thanks to the other members of the gR initiative, in particular to David Edwards for providing functions for formula-manipulation.

References

```
Hojsgaard, S., Edwards, D., Lauritzen, S. (2012) Graphical models with R. Springer. ISBN: 978-1-4614-2298-3
```

Lauritzen, S. L. (2002). gRaphical Models in R. R News, 3(2)39.

grbase-utilities

gRbase utilities

Description

Various utility functions for gRbase. Includes 'faster versions' of certain standard R functions.

Usage

```
rhsFormula2list(form)
rhsf2list(form)
rhsf2vec(form)
listify_dots(dots)
list2rhsFormula(form)
list2rhsf(form)
rowmat2list(X)
colmat2list(X)
matrix2list(X, byrow = TRUE)
which.arr.index(X)
which_matrix_index(X)
```

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```
rowSumsPrim(X)

colSumsPrim(X)

colwiseProd(v, X)

lapplyV2I(setlist, item)

lapplyI2V(setlist, item)
```

Arguments

form Formula specification (a right-hand sided formula, a numeric/character vector

or a list of vectors).

dots dot-arguments to be turned into a list

X A matrix.

byrow Should the split be by row or by column.

v A vector.

setlist A list of atomic vectors

item An atomic vector

Details

which.arr.ind: Returns matrix n x 2 matrix with indices of non-zero entries in matrix X. Notice which_matrix_index__ is cpp implementation.

colwiseProd: multiplies a vector v and a matrix X columnwise (as opposed to rowwise which is achieved by v * X). Hence colwiseProd does the same as t(v * t(X)) - but it does so faster for numeric values.

- lapplyV2I: same as but much faster than lapply(setlist, function(elt) match(elt, item))
- lapplyI2V: same as but faster than lapply(setlist, function(elt) item[elt])

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
## colwiseProd
X <- matrix(1:16, nrow=4)
v <- 1:4
t(v * t(X))
colwiseProd(v, X)
## Not run:
system.time(for (ii in 1:100000) t(v * t(X)))
system.time(for (ii in 1:100000) colwiseProd(v, X))
## End(Not run)</pre>
```

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```
setlist <- list(c(1,2,3), c(2,3,4), c(2,4,5))
item <- c(2,3)

lapplyV2I(setlist, item)
lapply(setlist, function(gg) match(gg, item))

lapplyI2V(setlist, item)
lapply(setlist, function(x) item[x])

if (require(microbenchmark)){
microbenchmark(
  lapplyV2I(setlist, item),
  lapply(setlist, function(elt) match(elt, item)))

microbenchmark::microbenchmark(
  lapplyI2V(setlist, item),
  lapply(setlist, function(elt) item[elt]))
}</pre>
```

grbase_generics

Compile and propagate functions

Description

compile and propagate are generic functions which invoke particular methods which depend on the class of the first argument

Usage

```
fit(object, ...)
compile(object, ...)
propagate(object, ...)
stepwise(object, ...)
```

Arguments

object An object

... Additional arguments which depends on the class of the object

Value

The value returned depends on the class of the first argument.

70 set-operations

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

References

Højsgaard, Søren; Edwards, David; Lauritzen, Steffen (2012): Graphical Models with R, Springer

internal

Internal functions for the gRbase package

Description

These functions are not intended to be called directly.

set-operations

Suite of set operations

Description

Set operations for gRbase and related packages.

Usage

```
maximal_sets(setlist, index = FALSE)
minimal_sets(setlist, index = FALSE)
remove_redundant(setlist, maximal = TRUE, index = FALSE)
is_inset(x, setlist, index = FALSE)
get_subset(x, setlist, all = FALSE)
get_superset(x, setlist, all = FALSE)
is_subsetof(set, set2)
is_subsetof(x, set)
subsetof(x, set)
```

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Arguments

setlist	List of vectors (representing a set of subsets)
index	Logical; should indices (in setlist) be returned or a set of subsets.
maximal	Logical; see section 'Details' for a description.
x, set, set2	Vector representing a set.
all	Logical; see section 'Details' for a description.

Details

'setlist' is a list of vectors representing a set of subsets; i.e. V1,...VQ where Vk is a subset of some base set V.

'all' If true, get_superset will return index of all vectors containing the element; otherwise only the first index is returned.

is_inset: Checks if the set x is in one of the Vk's.

remove_redundant: Returns those Vk which are not contained in other subsets; i.e. gives the maximal sets. If maximal is FALSE then returns the minimal sets; i.e. Vk is returned if Vk is contained in one of the other sets Vl and there are no set Vn contained in Vk.

Notice that the comparisons are made by turning the elements into characters and then comparing these. Hence 1 is identical to "1".

Author(s)

Søren Højsgaard, <sorenh@math.aau.dk>

Examples

```
set <- list(c(1, 2), c(1, 2, 3), c(2, 3, 6), c(2, 4), c(5, 6), 5)
el1 < -c(2, 1)
el2 <- c(2, 3)
el3 < -c(4, 3)
el4 < -c(2, 1, 3)
maximal_sets(set)
minimal_sets(set)
remove_redundant(set)
remove_redundant(set, maximal=FALSE)
is_inset(el1, set)
is_inset(el2, set)
is_inset(el3, set)
get_subset(el1, set)
get_subset(el1, set)
get_subset(el2, set)
get_subset(el3, set)
```

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```
get_superset(el1, set)
get_superset(el1, set, all=TRUE)
get_superset(el2, set)
get_superset(el3, set)

is_subsetof(el1, el1)
is_subsetof(el1, el2)
is_subsetof(el1, el4)
```

ug2dag

Coerce between undirected and directed graphs when possible

Description

An undirected graph G can be converted to a dag if G is chordal.

Usage

```
ug2dag(object)
```

Arguments

object

An igraph object.

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