Package 'grpSLOPE'

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Type Package

Title Group Sorted L1 Penalized Estimation

Version 0.3.3

Description Group SLOPE (Group Sorted L1 Penalized Estimation) is
a penalized linear regression method that is used for adaptive
selection of groups of significant predictors in a high-dimensional
linear model. The Group SLOPE method can control the (group) false
discovery rate at a user-specified level (i.e., control the expected
proportion of irrelevant among all selected groups of predictors).
For additional information about the implemented methods please see
Brzyski, Gossmann, Su, Bogdan (2018) <doi:10.1080/01621459.2017.1411269>.

License GPL-3

URL https://github.com/agisga/grpSLOPE

BugReports https://github.com/agisga/grpSLOPE/issues

LinkingTo Rcpp

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R topics documented:

`admmSolverGroupSLOPE` *Alternating direction method of multipliers*

Description

Compute the coefficient estimates for the Group SLOPE problem.

Usage

```
admmSolverGroupSLOPE(
  y,
  A,
  group,
  wt,
  lambda,
  rho = NULL,
  max.iter = 10000,
  verbose = FALSE,
  absolute.tol = 1e-04,
```

```
  relative.tol = 1e-04,
  z.init = NULL,
  u.init = NULL,
  ...
)
```

Arguments

y	the response vector
A	the model matrix
group	A vector describing the grouping structure. It should contain a group id for each predictor variable.
wt	A vector of weights (per coefficient)
lambda	A decreasing sequence of regularization parameters λ
rho	Penalty parameter in the augmented Lagrangian (see Boyd et al., 2011)
max.iter	Maximal number of iterations to carry out
verbose	A logical specifying whether to print output or not
absolute.tol	The absolute tolerance used in the stopping criteria for the primal and dual feasibility conditions (see Boyd et al., 2011, Sec. 3.3.1)
relative.tol	The relative tolerance used in the stopping criteria for the primal and dual feasibility conditions (see Boyd et al., 2011, Sec. 3.3.1)
z.init	An optional initial value for the iterative algorithm
u.init	An optional initial value for the iterative algorithm
...	Options passed to prox_sorted_L1

Details

admmSolverGroupSLOPE computes the coefficient estimates for the Group SLOPE model. The employed optimization algorithm is the alternating direction method of multipliers (ADMM).

Value

A list with the entries:

x Solution (n-by-1 matrix)

status Convergence status: 1 if optimal, 2 if iteration limit reached

iter Number of iterations of the ADMM method

References

S. Boyd, N. Parikh, E. Chu, B. Peleato, and J. Eckstein (2011) *Distributed Optimization and Statistical Learning via the Alternating Direction Method of Multipliers.* Foundations and Trends in Machine Learning 3 (1).

Examples

```
set.seed(1)
A   <- matrix(runif(100, 0, 1), 10, 10)
grp <- c(0, 0, 1, 1, 2, 2, 2, 2, 2, 3)
wt  <- c(2, 2, 2, 2, 5, 5, 5, 5, 5, 1)
x   <- c(0, 0, 5, 1, 0, 0, 0, 1, 0, 3)
y   <- A %*% x
lam <- 0.1 * (10:7)
result <- admmSolverGroupSLOPE(y = y, A = A, group = grp, wt = wt,
                               lambda=lam, rho = 1, verbose = FALSE)
result$x
#           [,1]
#  [1,] 0.000000
#  [2,] 0.000000
#  [3,] 3.856002
#  [4,] 2.080742
#  [5,] 0.000000
#  [6,] 0.000000
#  [7,] 0.000000
#  [8,] 0.000000
#  [9,] 0.000000
# [10,] 3.512829
```

---

coef.grpSLOPE *Extract model coefficients*

Description

Extract the regression coefficients from a grpSLOPE object, either on the scale of the normalized design matrix (i.e., columns centered and scaled to unit norm), or on the original scale.

Usage

```
## S3 method for class 'grpSLOPE'
coef(object, scaled = TRUE, ...)
```

Arguments

object	A grpSLOPE object
scaled	Should the coefficients be returned for the normalized version of the design matrix?
...	Potentially further arguments passed to and from methods

Details

If `scaled` is set to `TRUE`, then the coefficients are returned for the normalized version of the design matrix, which is the scale on which they were computed. If `scaled` is set to `FALSE`, then the coefficients are transformed to correspond to the original (unaltered) design matrix. In case that `scaled = FALSE`, an estimate for the intercept term is returned with the other coefficients. In case that `scaled = TRUE`, the estimate of the intercept is always equal to zero, and is not explicitly provided.

Value

A named vector of regression coefficients where the names signify the group that each entry belongs to

Examples

```
set.seed(1)
A   <- matrix(rnorm(100^2), 100, 100)
grp <- rep(rep(letters[1:20]), each=5)
b   <- c(rep(1, 20), rep(0, 80))
y   <- A %*% b + rnorm(10)
result <- grpSLOPE(X=A, y=y, group=grp, fdr=0.1)
head(coef(result), 8)
#       a_1       a_2       a_3       a_4       a_5       b_1       b_2       b_3
#  7.942177  7.979269  8.667013  8.514861 10.026664  8.963364 10.037355 10.448692
head(coef(result, scaled = FALSE), 8)
# (Intercept)        a_1        a_2        a_3        a_4        a_5        b_1        b_2
# -0.4418113  0.8886878  0.8372108  0.8422089  0.8629597  0.8615827  0.9323849  0.9333445
```

---

getGroupID *Get a groupID object*

Description

Mostly intended for internal use.

Usage

```
getGroupID(group)
```

Arguments

`group`	A vector describing the grouping structure. It should contain a group id for each predictor variable.

Value

An object of class groupID, which is a list, whose members are vectors of indices corresponding to each group. The names of the list members are the corresponding group names.

Examples

```
group  <- c("A", "A", 2, 9, "A", 9, 9, 2, "A")
group.id <- getGroupID(group)
group.id
# $A
# [1] 1 2 5 9
#
# $`2`
# [1] 3 8
#
# $`9`
# [1] 4 6 7
#
# attr(,"class")
# [1] "groupID"
```

---

grpSLOPE *Group SLOPE (Group Sorted L-One Penalized Estimation)*

Description

Performs selection of significant groups of predictors and estimation of the corresponding coefficients using the Group SLOPE method (see Brzyski et. al., 2016).

Usage

```
grpSLOPE(
  X,
  y,
  group,
  fdr,
  lambda = "corrected",
  sigma = NULL,
  verbose = FALSE,
  orthogonalize = NULL,
  normalize = TRUE,
  max.iter = 10000,
  dual.gap.tol = 1e-06,
  infeas.tol = 1e-06,
  x.init = NULL,
  ...
)
```

Arguments

X	The model matrix
y	The response variable

group	A vector describing the grouping structure. It should contain a group id for each predictor variable.
fdr	Target group false discovery rate (gFDR)
lambda	Method used to obtain the regularizing sequence lambda. Possible values are "max", "mean", and "corrected" (default). See lambdaGroupSLOPE for detail. Alternatively, any non-increasing sequence of the correct length can be passed.
sigma	Noise level. If ommited, estimated from the data, using Procedure 2 in Brzyski et. al. (2016).
verbose	A logical specifying whether to print output or not
orthogonalize	Whether to orthogonalize the model matrix within each group. Do not set manually unless you are certain that your data is appropriately pre-processed.
normalize	Whether to center the input data and re-scale the columns of the design matrix to have unit norms. Do not disable this unless you are certain that your data are appropriately pre-processed.
max.iter	See proximalGradientSolverGroupSLOPE.
dual.gap.tol	See proximalGradientSolverGroupSLOPE.
infeas.tol	See proximalGradientSolverGroupSLOPE.
x.init	See proximalGradientSolverGroupSLOPE.
...	Options passed to prox_sorted_L1

Details

Multiple methods are available to generate the regularizing sequence lambda, see lambdaGroupSLOPE for detail. The model matrix is transformed by orthogonalization within each group (see Section 2.1 in Brzyski et. al., 2016), and penalization is imposed on $\|X_{I_i}\beta_{I_i}\|$. When orthogonalize = TRUE, due to within group orthogonalization, the solution vector beta cannot be computed, if a group submatrix does not have full column rank (e.g., if there are more predictors in a selected group than there are observations). In that case only the solution vector c of the transformed (orthogonalized) model is returned. Additionally, in any case the vector group.norms is returned with its ith entry being $\|X_{I_i}\beta_{I_i}\|$, i.e., the overall effect of each group. Note that all of these results are returned on the scale of the normalized versions of X and y. However, original.scale contains the regression coefficients transformed to correspond to the original (unaltered) X and y. In that case, an estimate for the intercept term is also returned with the other coefficients in original.scale (while on the normalized scale the estimate of the intercept is always equal to zero, and is not explicitly provided in the grpSLOPE output).

Value

A list with members:

beta Solution vector. See Details.

c Solution vector of the transformed model. See Details.

group.norms Overall effect of each group. See Details.

selected Names of selected groups (i.e., groups of predictors with at least one non-zero coefficient estimate)

optimal Convergence status

iter Iterations of the proximal gradient method

lambda Regularizing sequence

lambda.method Method used to construct the regularizing sequence

sigma (Estimated) noise level

group The provided grouping structure (corresponding to `beta`)

group.c Grouping structure of the transformed model (corresponding to `c`)

original.scale A list containing the estimated intercept and regression coefficients on the original scale. See Details.

References

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2016) *Group SLOPE – adaptive selection of groups of predictors*, https://arxiv.org/abs/1610.04960

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2019) *Group SLOPE – adaptive selection of groups of predictors*. Journal of the American Statistical Association 114 (525): 419–33.

Examples

```
# generate some data
set.seed(1)
A   <- matrix(rnorm(100^2), 100, 100)
grp <- rep(rep(1:20), each=5)
b   <- c(runif(20), rep(0, 80))
# (i.e., groups 1, 2, 3, 4, are truly significant)
y   <- A %*% b + rnorm(10)
fdr <- 0.1 # target false discovery rate
# fit a Group SLOPE model
result <- grpSLOPE(X=A, y=y, group=grp, fdr=fdr)
result$selected
# [1] "1"  "2"  "3"  "4"  "14"
result$sigma
# [1] 0.7968632
head(result$group.norms)
#         1         2         3         4         5         6
#  2.905449  5.516103  8.964201 10.253792  0.000000  0.000000
```

`lambdaGroupSLOPE` *Regularizing sequence for Group SLOPE*

Description

Generate the regularizing sequence `lambda` for the Group SLOPE problem according to one of multiple methods (see Details).

Usage

```
lambdaGroupSLOPE(method, fdr, group, wt, n.obs = NULL)
```

Arguments

method	Possible values are "max", "mean", and "corrected". See under Details.
fdr	Target group false discovery rate (gFDR)
group	A vector describing the grouping structure. It should contain a group id for each predictor variable.
wt	A named vector of weights, one weight per group of predictors (named according to names as in vector group)
n.obs	Number of observations (i.e., number of rows in A); required only if method is "corrected"

Details

Multiple methods are available to generate the regularizing sequence lambda:

- "max" – lambdas as in Theorem 2.5 in Brzyski et. al. (2016). Provalby controls gFDR in orthogonal designs.
- "mean" – lambdas of equation (2.16) in Brzyski et. al. (2016). Applicable for gFDR control in orthogonal designs. Less conservative than "max".
- "corrected" – lambdas of Procedure 1 in Brzyski et. al. (2016); in the special case that all group sizes are equal and wt is a constant vector, Procedure 6 of Brzyski et. al. (2016) is applied. Applicable for gFDR control when predictors from different groups are stochastically independent.

Value

A vector containing the calculated lambda values.

References

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2016) *Group SLOPE – adaptive selection of groups of predictors*, https://arxiv.org/abs/1610.04960

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2019) *Group SLOPE – adaptive selection of groups of predictors*. Journal of the American Statistical Association 114 (525): 419–33.

Examples

```
# specify 6 groups of sizes 2, 3, and 4
group <- c(1, 1, 2, 2, 2, 3, 3, 3, 3,
           4, 4, 5, 5, 5, 6, 6, 6, 6)
# set the weight for each group to the square root of the group's size
wt <- rep(c(sqrt(2), sqrt(3), sqrt(4)), 2)
names(wt) <- 1:6
# compute different lambda sequences
lambda.max <- lambdaGroupSLOPE(method="max", fdr=0.1, group=group, wt=wt)
```

```
lambda.mean <- lambdaGroupSLOPE(method="mean", fdr=0.1, group=group, wt=wt)
lambda.corrected <- lambdaGroupSLOPE(method="corrected", fdr=0.1,
                                     group=group, wt=wt, n.obs=1000)
rbind(lambda.max, lambda.mean, lambda.corrected)
#                      [,1]     [,2]     [,3]     [,4]     [,5]     [,6]
# lambda.max       2.023449 1.844234 1.730818 1.645615 1.576359 1.517427
# lambda.mean      1.880540 1.723559 1.626517 1.554561 1.496603 1.447609
# lambda.corrected 1.880540 1.729811 1.637290 1.568971 1.514028 1.467551
```

`predict.grpSLOPE` *Obtain predictions*

Description

Obtain predictions from a `grpSLOPE` model on new data

Usage

```
## S3 method for class 'grpSLOPE'
predict(object, newdata, ...)
```

Arguments

`object`	A `grpSLOPE` object
`newdata`	Predictor variables arranged in a matrix
`...`	Potentially further arguments passed to and from methods

Details

Note that `newdata` must contain the same predictor variables as columns in the same order as the design matrix `X` that was used for the `grpSLOPE` model fit.

Value

A vector of length nrow(newdata) containing the resulting predictions.

Examples

```
set.seed(1)
A   <- matrix(rnorm(100^2), 100, 100)
grp <- rep(rep(1:20), each = 5)
b   <- c(rep(1, 20), rep(0, 80))
y   <- A %*% b + rnorm(10)
result <- grpSLOPE(X = A, y = y, group = grp, fdr = 0.1)
newdata <- matrix(rnorm(800), 8, 100)
# group SLOPE predictions:
predict(result, newdata)
# [1] -5.283385 -6.313938 -3.173068  1.901488  9.796677 -0.144516 -0.611164 -5.167620
```

```
# true mean values:
as.vector(newdata %*% b)
# [1] -5.0937160 -6.5814111 -3.5776124  2.7877449 11.0668777  1.0253236 -0.4261076 -4.8622940
```

---

proxGroupSortedL1 *Prox for group SLOPE*

Description

Evaluate the proximal mapping for the group SLOPE problem.

Usage

```
proxGroupSortedL1(y, group, lambda, ...)
```

Arguments

y	The response vector
group	Either a vector or an object of class groupID (e.g., as produced by getGroupID), which is describing the grouping structure. If it is a vector, then it should contain a group id for each predictor variable.
lambda	A decreasing sequence of regularization parameters λ
...	Options passed to prox_sorted_L1

Details

proxGroupSortedL1 evaluates the proximal mapping of the group SLOPE problem by reducing it to the prox for the (regular) SLOPE and then applying the fast prox algorithm for the Sorted L1 norm.

Value

The solution vector.

References

M. Bogdan, E. van den Berg, C. Sabatti, W. Su, E. Candes (2015), *SLOPE – Adaptive variable selection via convex optimization*, https://arxiv.org/abs/1407.3824

Examples

```
grp <- c(0,0,0,1,1,0,2,1,0,2)
proxGroupSortedL1(y = 1:10, group = grp, lambda = c(10, 9, 8))
#  [1] 0.2032270 0.4064540 0.6096810 0.8771198 1.0963997 1.2193620 1.3338960
#  [8] 1.7542395 1.8290430 1.9055657
```

`proximalGradientSolverGroupSLOPE` *Proximal gradient method for Group SLOPE*

Description

Compute the coefficient estimates for the Group SLOPE problem.

Usage

```
proximalGradientSolverGroupSLOPE(
  y,
  A,
  group,
  wt,
  lambda,
  max.iter = 10000,
  verbose = FALSE,
  dual.gap.tol = 1e-06,
  infeas.tol = 1e-06,
  x.init = NULL,
  ...
)
```

Arguments

`y`	the response vector
`A`	the model matrix
`group`	A vector describing the grouping structure. It should contain a group id for each predictor variable.
`wt`	A vector of weights (per coefficient)
`lambda`	A decreasing sequence of regularization parameters λ
`max.iter`	Maximal number of iterations to carry out
`verbose`	A `logical` specifying whether to print output or not
`dual.gap.tol`	The tolerance used in the stopping criteria for the duality gap
`infeas.tol`	The tolerance used in the stopping criteria for the infeasibility
`x.init`	An optional initial value for the iterative algorithm
`...`	Options passed to `prox_sorted_L1`

Details

`proximalGradientSolverGroupSLOPE` computes the coefficient estimates for the Group SLOPE model. The employed optimization algorithm is FISTA with backtracking Lipschitz search.

Value

A list with the entries:

x Solution (n-by-1 matrix)

status Convergence status: 1 if optimal, 2 if iteration limit reached

L Approximation of the Lipschitz constant (step size)

iter Iterations of the proximal gradient method

L.iter Total number of iterations spent in Lipschitz search

References

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2016) *Group SLOPE – adaptive selection of groups of predictors*, https://arxiv.org/abs/1610.04960

D. Brzyski, A. Gossmann, W. Su, and M. Bogdan (2019) *Group SLOPE – adaptive selection of groups of predictors*. Journal of the American Statistical Association 114 (525): 419–33. doi:10.1080/01621459.2017.1411269

A. Gossmann, S. Cao, Y.-P. Wang (2015) *Identification of Significant Genetic Variants via SLOPE, and Its Extension to Group SLOPE*. In Proceedings of ACM BCB 2015. doi:10.1145/2808719.2808743

Examples

```
set.seed(1)
A   <- matrix(runif(100, 0, 1), 10, 10)
grp <- c(0, 0, 1, 1, 2, 2, 2, 2, 2, 3)
wt  <- c(2, 2, 2, 2, 5, 5, 5, 5, 5, 1)
x   <- c(0, 0, 5, 1, 0, 0, 0, 1, 0, 3)
y   <- A %*% x
lam <- 0.1 * (10:7)
result <- proximalGradientSolverGroupSLOPE(y=y, A=A, group=grp, wt=wt, lambda=lam, verbose=FALSE)
result$x
#           [,1]
#  [1,] 0.000000
#  [2,] 0.000000
#  [3,] 3.856005
#  [4,] 2.080736
#  [5,] 0.000000
#  [6,] 0.000000
#  [7,] 0.000000
#  [8,] 0.000000
#  [9,] 0.000000
# [10,] 3.512833
```

prox_sorted_L1 *Prox for sorted L1 norm*

Description

Compute the prox for the sorted L1 norm. That is, given a vector x and a decreasing vector λ, compute the unique value of y minimizing

$$\frac{1}{2}\|x-y\|_2^2 + \sum_{i=1}^{n} \lambda_i |x|_{(i)}.$$

At present, two methods for computing the sorted L1 prox are supported. By default, we use a fast custom C implementation. Since SLOPE can be viewed as an isotonic regression problem, the prox can also be computed using the `isotone` package. This option is provided primarily for testing.

Usage

```
prox_sorted_L1(x, lambda, method = c("c", "isotone"))
```

Arguments

`x`	input vector
`lambda`	vector of λ's, sorted in decreasing order
`method`	underlying prox implementation, either 'c' or 'isotone' (see Details)

Details

This function has been adapted (with only cosmetic changes) from the R package `SLOPE` version 0.1.3, due to this function being deprecated and defunct in `SLOPE` versions which are newer than 0.1.3.

Value

The solution vector y.

sigma *Extract (estimated) noise level*

Description

Extract the noise level of the `grpSLOPE` model.

Usage

```
## S3 method for class 'grpSLOPE'
sigma(object, ...)
```

Arguments

object	A grpSLOPE object
...	Potentially further arguments passed to and from methods

Details

This basically obtains object$sigma. For R (>= 3.3.0) sigma is an S3 method with the default method coming from the stats package.

Value

The noise level of the given grpSLOPE model. A number.

Examples

```
set.seed(1)
A   <- matrix(rnorm(100^2), 100, 100)
grp <- rep(rep(1:20), each = 5)
b   <- c(rep(1, 20), rep(0, 80))
y   <- A %*% b + rnorm(10)
# model with unknown noise level
result <- grpSLOPE(X = A, y = y, group = grp, fdr = 0.1)
sigma(result)
# [1] 0.6505558
# model with known noise level
result <- grpSLOPE(X = A, y = y, group = grp, fdr = 0.1, sigma = 1)
sigma(result)
# [1] 1
```

SLOPE_solver *Sorted L1 solver*

Description

Solves the sorted L1 penalized regression problem: given a matrix A, a vector b, and a decreasing vector λ, find the vector x minimizing

$$\frac{1}{2}\|Ax - b\|_2^2 + \sum_{i=1}^{p} \lambda_i |x|_{(i)}.$$

This optimization problem is convex and is solved using an accelerated proximal gradient descent method.

Usage

```
SLOPE_solver(
  A,
  b,
  lambda,
  initial = NULL,
  prox = prox_sorted_L1,
  max_iter = 10000,
  grad_iter = 20,
  opt_iter = 1,
  tol_infeas = 1e-06,
  tol_rel_gap = 1e-06
)
```

Arguments

A	an n-by-p matrix
b	vector of length n
lambda	vector of length p, sorted in decreasing order
initial	initial guess for x
prox	function that computes the sorted L1 prox
max_iter	maximum number of iterations in the gradient descent
grad_iter	number of iterations between gradient updates
opt_iter	number of iterations between checks for optimality
tol_infeas	tolerance for infeasibility
tol_rel_gap	tolerance for relative gap between primal and dual problems

Details

This function has been adapted (with only cosmetic changes) from the R package SLOPE version 0.1.3, due to this function being deprecated and defunct in SLOPE versions which are newer than 0.1.3.

Value

An object of class SLOPE_solver.result. This object is a list containing at least the following components:

x	solution vector x
optimal	logical: whether the solution is optimal
iter	number of iterations

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