

# Package ‘latte’

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**Type** Package

**Title** Interface to 'LattE' and '4ti2'

**Version** 0.2.1

**Maintainer** David Kahle <david@kahle.io>

**Description** Back-end connections to 'LattE' (<<https://www.math.ucdavis.edu/~latte>>) for counting lattice points and integration inside convex polytopes and '4ti2' (<<http://www.4ti2.de/>>) for algebraic, geometric, and combinatorial problems on linear spaces and front-end tools facilitating their use in the 'R' ecosystem.

**License** GPL-2

**URL** <https://github.com/dkahle/latte>

**BugReports** <https://github.com/dkahle/latte/issues>

**LazyData** TRUE

**SystemRequirements** LattE <<https://www.math.ucdavis.edu/~latte/>>, 4ti2  
<<http://www.4ti2.de/>>

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glue

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**Author** David Kahle [aut, cph, cre] (<<https://orcid.org/0000-0002-9999-1558>>),  
Luis Garcia [aut, cph],  
Ruriko Yoshida [aut, cph]

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genmodel	<i>Generate a configuration matrix</i>
----------	--

---

### Description

genmodel runs 4ti2's genmodel program to compute the configuration matrix A corresponding to graphical statistical models given by a simplicial complex and levels on the nodes.

### Usage

```
genmodel(varlvs, facets, dir = tempdir(), quiet = TRUE,
        shell = FALSE, ...)
```

### Arguments

varlvs	a vector containing the number of levels of each variable
facets	the facets generating the hierarchical model, a list of vectors of variable indices
dir	Directory to place the files in, without an ending /
quiet	If FALSE, messages the 4ti2 output
shell	Messages the shell code used to do the computation
...	Additional arguments to pass to the function

### Value

The configuration matrix of the model provided

## Examples

```
if (has_4ti2()) {  
  
    varlvs <- rep(2, 2)  
    facets <- list(1, 2)  
    genmodel(varlvs, facets)  
    genmodel(varlvs, facets, quiet = FALSE)  
  
    varlvs <- rep(3, 3)  
    facets <- list(1:2, 2:3, c(3,1))  
    genmodel(varlvs, facets)  
  
    # compare this to algstat's hmat function  
  
}
```

---

kprod

*Iterated Kronecker product*

---

## Description

Compute the Kronecker product of several matrices.

## Usage

```
kprod(..., FUN = `*`)
```

## Arguments

...	A listing of matrices
FUN	A function to pass to <a href="#">kronecker()</a>

## Details

If kronecker is the function that computes  $A \times B$ , kprod computes  $A \times B \times C$  and so on; it's a wrapper of Reduce and kronecker.

## Value

A matrix that is the kronecker product of the specified matrices (from left to right).

## Examples

```
kprod(diag(2), t(ones(2)))
kprod(t(ones(2)), diag(2))

kprod(diag(2), t(ones(2)), t(ones(2)))
kprod(t(ones(2)), diag(2), t(ones(2)))
kprod(t(ones(2)), t(ones(2)), diag(2))

# cf. aoki, hara, and takemura p.13
rbind(
  kprod(diag(2), t(ones(2))),
  kprod(t(ones(2)), diag(2))
)
```

latte

*R Interface to LattE and 4ti2*

## Description

Back-end connections to LattE (<https://www.math.ucdavis.edu/~latte/>) and 4ti2 (<http://www.4ti2.de/>) executables and front-end tools facilitating their use in the R ecosystem.

latte-count

*Count integer points in a polytope*

## Description

`latte_count` uses LattE's count function to count the (integer) lattice points in a polytope and compute Ehrhart polynomials.

## Usage

```
count_core(spec, dir = tempdir(), quiet = TRUE, mpoly = TRUE, ...)
latte_count(spec, dir = tempdir(), quiet = TRUE, mpoly = TRUE, ...)
latte_fcount(spec, dir = tempdir(), quiet = TRUE, mpoly = TRUE, ...)
```

## Arguments

spec	Specification, see details and examples
dir	Directory to place the files in, without an ending /
quiet	Show latte output?
mpoly	When opts = "ehrhart-polynomial", return the mpoly version of it
...	Additional arguments to pass to the function, see count --help at the command line to see examples. Note that dashes - should be specified with underscores _

## Details

The specification should be one of the following: (1) a character string or strings containing an inequality in the mpoly expression format (see examples), (2) a list of vertices, (3) a list of A and b for the equation Ax <= b (see examples), or (4) raw code for LattE's count program. If a character vector is supplied, (1) and (4) are distinguished by the number of strings.

Behind the scenes, count works by writing a latte file and running count on it. If a specification other than a length one character is given to it (which is considered to be the code), count attempts to convert it into LattE code and then run count on it.

## Value

The count. If the count is a number has less than 10 digits, an integer is returned. If the number has 10 or more digits, an integer in a character string is returned. You may want to use the gmp package's as.bigz to parse it.

## Examples

```
if (has_latte()) {

  spec <- c("x + y <= 10", "x >= 1", "y >= 1")
  latte_count(spec) # 45
  latte_count(spec, quiet = FALSE) # 45
  latte_count(spec, dilation = 10) # 3321
  latte_count(spec, homog = TRUE) # 45

  # by default, the output from LattE is in
  list.files(tempdir())
  list.files(tempdir(), recursive = TRUE)

  # ehrhart polynomials
  latte_count(spec, ehrhart_polynomial = TRUE)
  latte_count(spec, ehrhart_polynomial = TRUE, mpoly = FALSE)

  # ehrhart series (raw since mpoly can't handle rational functions)
  latte_count(spec, ehrhart_series = TRUE)

  # simplified ehrhart series - not yet implemented
  #latte_count(spec, simplified_ehrhart_polynomial = TRUE)
```

```

# first terms of the ehrhart series
latte_count(spec, ehrhart_taylor = 1)
latte_count(spec, ehrhart_taylor = 2)
latte_count(spec, ehrhart_taylor = 3)
latte_count(spec, ehrhart_taylor = 4)

# multivariate generating function
latte_count(spec, multivariate_generating_function = TRUE)

# by vertices
spec <- list(c(1,1), c(10,1), c(1,10), c(10,10))
latte_count(spec)
latte_count(spec, vrep = TRUE)

code <- "
5 3
1 -1  0
1  0 -1
1 -1 -1
0  1  0
0  0  1
"
latte_count(code)

# for Ax <= b, see this example from the latte manual p.10
A <- matrix(c(
  1,  0,
  0,  1,
  1,  1,
 -1,  0,
  0, -1
), nrow = 5, byrow = TRUE)
b <- c(1, 1, 1, 0, 0)
latte_count(list(A = A, b = b))

}


```

## Description

`format_latte()` formats a matrix in latte's style. `write_latte()` writes a latte-formatted file to file. `read_latte()` reads a latte-formatted file from disk.

## Usage

```
format_latte(mat, file)

write_latte(mat, file)

write.latte(mat, file)

read_latte(file, format = c("mat", "Ab"))

read.latte(file, format = c("mat", "Ab"))
```

## Arguments

mat	A matrix
file	A filename
format	"mat" or "Ab"

## Value

- `format_latte()` – A character string of the matrix in latte format.
- `write_latte()` – An invisible character string of the formatted output.
- `read_latte()` – An integer matrix.

## Examples

```
(mat <- matrix(sample(9), 3, 3))

format_latte(mat)
cat(format_latte(mat))

(file <- file.path(tempdir(), "foo.hrep"))
write_latte(mat, file)
file.show(file)
read_latte(file)
read_latte(file, "Ab")

attr(mat, "linearity") <- c(1, 3)
attr(mat, "nonnegative") <- 2
mat
format_latte(mat)
cat(format_latte(mat))
write_latte(mat, file)
```

```
file.show(file)
read_latte(file)

file.remove(file)
```

**latte-optim***Solve an integer program with LattE***Description**

`latte_max` and `latte_min` use LattE's `latte-maximize` and `latte-minimize` functions to find the maximum or minimum of a linear objective function over the integers points in a polytope (i.e. satisfying linearity constraints). This makes use of the digging algorithm; see the LattE manual at <http://www.math.ucdavis.edu/~latte> for details.

**Usage**

```
latte_optim(objective, constraints, type = c("max", "min"),
            method = c("lp", "cones"), dir = tempdir(), opts = "",
            quiet = TRUE, shell = FALSE)

latte_max(objective, constraints, method = c("lp", "cones"),
           dir = tempdir(), opts = "", quiet = TRUE)

latte_min(objective, constraints, method = c("lp", "cones"),
           dir = tempdir(), opts = "", quiet = TRUE)
```

**Arguments**

<code>objective</code>	A linear polynomial to pass to <code>mp()</code> , see examples
<code>constraints</code>	A collection of linear polynomial (in)equalities that define the feasibility region, the integers in the polytope
<code>type</code>	"max" or "min"
<code>method</code>	Method "LP" or "cones"
<code>dir</code>	Directory to place the files in, without an ending /
<code>opts</code>	Options; see the LattE manual at <a href="http://www.math.ucdavis.edu/~latte">http://www.math.ucdavis.edu/~latte</a>
<code>quiet</code>	Show latte output
<code>shell</code>	Messages the shell code used to do the computation

**Value**

A named list with components `par`, a named-vector of optimizing arguments, and `value`, the value of the objective function at the optimial point.

## Examples

```

if (has_latte()) {

latte_max(
  "-2 x + 3 y",
  c("x + y <= 10", "x >= 0", "y >= 0")
)

latte_max(
  "-2 x + 3 y",
  c("x + y <= 10", "x >= 0", "y >= 0"),
  quiet = FALSE
)

df <- expand.grid("x" = 0:10, "y" = 0:10)
df <- subset(df, x + y <= 10L)
df$objective <- with(df, -2*x + 3*y)
library("ggplot2")
ggplot(df, aes(x, y, size = objective)) +
  geom_point()

latte_min(
  "-2 x + 3 y",
  c("x + y <= 10", "x >= 0", "y >= 0"),
  method = "cones"
)

latte_min("-2 x - 3 y - 4 z", c(
  "3 x + 2 y + z <= 10",
  "2 x + 5 y + 3 z <= 15",
  "x >= 0", "y >= 0", "z >= 0"
), "cones", quiet = FALSE)

}

```

## Description

4ti2 provides several executables that can be used to generate bases for a configuration matrix A. See the references for details.

## Usage

```
basis(exec, memoise = TRUE)

zbasis(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
       dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

markov(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
       dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

groebner(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
          dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

hilbert(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
        dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

graver(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
        dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

fzbasis(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
        dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

fmarkov(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
         dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

fgroebner(A, format = c("mat", "vec", "tab"), dim = NULL,
           all = FALSE, dir = tempdir(), quiet = TRUE, shell = FALSE,
           dbName = NULL, ...)

fhilbert(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
          dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)

fgraver(A, format = c("mat", "vec", "tab"), dim = NULL, all = FALSE,
         dir = tempdir(), quiet = TRUE, shell = FALSE, dbName = NULL, ...)
```

## Arguments

<code>exec</code>	don't use this parameter
<code>memoise</code>	don't use this parameter
<code>A</code>	The configuration matrix
<code>format</code>	How the basis (moves) should be returned. if "mat", the moves are returned as the columns of a matrix.
<code>dim</code>	The dimension to be passed to <code>vec2tab()</code> if format = "tab" is used; a vector of the number of levels of each variable in order

all	If TRUE, all moves (+ and -) are given. if FALSE, only the + moves are given as returned by the executable.
dir	Directory to place the files in, without an ending /
quiet	If FALSE, messages the 4ti2 output
shell	Messages the shell code used to do the computation
dbName	The name of the model in the markov bases database, <a href="http://markov-bases.de">http://markov-bases.de</a> , see examples
...	Additional arguments to pass to the function, e.g. p = "arb" specifies the flag -parb; not setting this issues a common warning

**Value**

a matrix containing the Markov basis as its columns (for easy addition to tables)

**References**

Drton, M., B. Sturmfels, and S. Sullivant (2009). *Lectures on Algebraic Statistics*, Basel: Birkhauser Verlag AG.

**Examples**

```

if (has_4ti2()) {

  # basic input and output for the 3x3 independence example
  (A <- rbind(
    kprod(diag(3), ones(1,3)),
    kprod(ones(1,3), diag(3))
  ))
  markov(A, p = "arb")

  # you can get the output formatted in different ways:
  markov(A, p = "arb", all = TRUE)
  markov(A, p = "arb", "vec")
  markov(A, p = "arb", "tab", c(3, 3))
  tableau(markov(A, p = "arb"), dim = c(3, 3)) # tableau notation

  # you can add options by listing them off
  # to see the options available to you by function,
  # go to http://www.4ti2.de
  markov(A, p = "arb")
}

```

```

# the basis functions are automatically cached for future use.
# (note that it doesn't persist across sessions.)
A <- rbind(
  kprod( diag(4), ones(1,4), ones(1,4)),
  kprod(ones(1,4), diag(4), ones(1,4)),
  kprod(ones(1,4), ones(1,4), diag(4))
)
system.time(markov(A, p = "arb"))
system.time(markov(A, p = "arb"))

# the un-cashed versions begin with an "f"
# (think: "forgetful" markov)
system.time(fmarkov(A, p = "arb"))
system.time(fmarkov(A, p = "arb"))

# you can see the command line code by typing shell = TRUE
# and the standard output with quiet = FALSE
# we illustrate these with fmarkov because otherwise it's cached
(A <- rbind(
  kprod(diag(2), ones(1,4)),
  kprod(ones(1,4), diag(2))
))
fmarkov(A, p = "arb", shell = TRUE)
fmarkov(A, p = "arb", quiet = FALSE)

# compare the bases for the 3x3x3 no-three-way interaction model
A <- rbind(
  kprod( diag(3), diag(3), ones(1,3)),
  kprod( diag(3), ones(1,3), diag(3)),
  kprod(ones(1,3), diag(3), diag(3))
)
str( zbasis(A, p = "arb")) # 8 elements = ncol(A) - qr(A)$rank
str( markov(A, p = "arb")) # 81 elements
str(groebner(A, p = "arb")) # 110 elements
str( graver(A)) # 795 elements

# the other bases are also cached
A <- rbind(
  kprod( diag(3), ones(1,3), ones(1,2)),
  kprod(ones(1,3), diag(3), ones(1,2)),
  kprod(ones(1,3), ones(1,3), diag(2))
)
system.time( graver(A))
system.time( graver(A))
system.time(fgraver(A))
system.time(fgraver(A))

```

```

# LAS ex 1.2.1, p.12 : 2x3 independence
(A <- rbind(
  kprod(diag(2), ones(1,3)),
  kprod(ones(1,2), diag(3))
))

markov(A, p = "arb", "tab", c(3, 3))
# Prop 1.2.2 says that there should be
2*choose(2, 2)*choose(3,2) # = 6
# moves (up to +-1)
markov(A, p = "arb", "tab", c(3, 3), TRUE)

# LAS example 1.2.12, p.17 (no 3-way interaction)
(A <- rbind(
  kprod( diag(2), diag(2), ones(1,2)),
  kprod( diag(2), ones(1,2), diag(2)),
  kprod(ones(1,2), diag(2), diag(2))
))
plot_matrix(A)
markov(A, p = "arb")
groebner(A, p = "arb")
graver(A)
tableau(markov(A, p = "arb"), dim = c(2,2,2))

# using the markov bases database, must be connected to internet
# commented out for predictable and fast cran checks time
# A <- markov(dbName = "ind3-3")
# B <- markov(rbind(
#   kprod(diag(3), ones(1,3)),
#   kprod(ones(1,3), diag(3))
# ), p = "arb")
# all(A == B)

# possible issues
# markov(diag(1, 10))
# zbasis(diag(1, 10), "vec")
# groebner(diag(1, 10), "vec", all = TRUE)
# graver(diag(1, 10), "vec", all = TRUE)
# graver(diag(1, 4), "tab", all = TRUE, dim = c(2,2))

```

---

}

---

**ones**

---

*Ones*

---

## Description

Make an array of ones

## Usage

`ones(...)`

## Arguments

...	A sequence of dimensions separated by commas
-----	--

## Value

An integer array of ones

## Examples

```
ones(5)
ones(5, 1)
ones(1, 5)
ones(2, 3)
ones(2, 3, 2)

str(ones(5))
```

---

**pathing**

---

*Set paths to LattE and 4ti2 executables*

---

## Description

These functions set the path to external programs either by (1) passing them a character string or (2) using `file.choose()`.

**Usage**

```
set_latte_path(path)

set_4ti2_path(path)

get_4ti2_path()

get_latte_path()

has_4ti2()

has_latte()

missing_4ti2_stop()

missing_latte_stop()
```

**Arguments**

path	A character string, the path to a 4ti2 function (e.g. markov) for setting 4ti2's path or a LattE function (e.g. count) for LattE's path
------	---

**Details**

When latte is loaded it attempts to find LattE and 4ti2 executables (represented by count and markov, respectively). How it looks depends on your operating system.

If you're using a Mac or Linux machine, it looks based on your system's path. Unfortunately, R changes the system path in such a way that the path that R sees is not the same as the path that you'd see if you were working in the terminal. (You can open the Terminal app on a Mac by going to /Applications/Utilities/Terminal.) Consequently, latte tries to guess the file in which your path is set. To do so, it first checks if your home directory (type echo ~/ in the terminal to figure out which directory this is if you don't know) for the file named .bash\_profile. If this file is present, it runs it and then checks your system's path variable (echo \$PATH). If it's not present, it does the same for .bashrc and then .profile. In any case, once it has its best guess at your path, it looks for "latte".

On Windows, latte just uses [Sys.which\(\)](#) on "whereis" to On Windows, latte just uses [Sys.which\(\)](#) on "whereis" to determine where the executables count and markov are (for LattE and 4ti2, respectively).

**Value**

An invisible character string, the path found. More importantly, the function has the side effect of setting the option "latte\_path" or "4ti2\_path"

**Author(s)**

David Kahle <david@kahle.io>

## Examples

```
has_4ti2()
if (has_4ti2()) get_4ti2_path()

has_latte()
if (has_4ti2()) get_latte_path()

# these are stored in your .Renviron file; that's where you should put the
# path to LattE and 4ti2 executables. for example, you should have a lines
# that look like
# LATTE=/Applications/latte/bin
# 4TI2=/Applications/latte/bin
# you can set these with usethis::edit_r_environ()

# you can change these in your current session with set_latte_path() and
# set_4ti2_path(), for example set_4ti2_path("/path/to/4ti2")
```

**plot-matrix**

*Plot a matrix*

## Description

`plot_matrix` is a R variant of Matlab's `spy` function.

## Usage

```
plot_matrix(A)
```

## Arguments

A	A matrix
---	----------

## Value

a ggplot object

## Author(s)

David Kahle <david@kahle.io>

## Examples

```
# the no-three-way interaction configuration
(A <- kprod(ones(1,3), diag(3), ones(3)))
plot_matrix(A)

if (has_4ti2()) {
  plot_matrix(markov(A))

  (A <- genmodel(c(2L, 2L), list(1L, 2L)))
  plot_matrix(A)
  plot_matrix(markov(A))

  (A <- genmodel(c(5L, 5L), list(1L, 2L)))
  plot_matrix(A)
  plot_matrix(markov(A))
}

}
```

ppi

*Compute the primitive partition identities*

## Description

ppi runs 4ti2's ppi program to compute the primitive partition identities, that is, the Graver basis of 1:N.

## Usage

```
ppi(N, dir = tempdir(), quiet = TRUE, shell = FALSE, ...)
```

## Arguments

N	A positive integer > 2
dir	Directory to place the files in, without an ending /
quiet	If FALSE, messages the 4ti2 output
shell	Messages the shell code used to do the computation
...	Additional arguments to pass to the function

## Value

A matrix containing the basis as its columns (for easy addition to tables)

**See Also**

[graver\(\)](#)

**Examples**

```
if (has_4ti2()) {  
  
  ppi(3)  
  t(ppi(3)) %*% 1:3  
  plot_matrix(ppi(3))  
  
  graver(t(1:3))  
  plot_matrix(graver(t(1:3)))  
  
  ppi(5, quiet = FALSE, shell = TRUE)  
  
}
```

<code>print.tableau</code>	<i>Pretty printing of tableau output.</i>
----------------------------	---

**Description**

Pretty printing of tableau output.

**Usage**

```
## S3 method for class 'tableau'  
print(x, ...)
```

**Arguments**

x	an object of class tableau
...	...

**Value**

Invisible string of the printed object.

**Examples**

```
# see ?tableau
```

---

qsolve*Solve a linear system over the rationals*

---

**Description**

qsolve runs 4ti2's qsolve program to compute the configuration matrix A corresponding to graphical statistical models given by a simplicial complex and levels on the nodes.

**Usage**

```
qsolve(mat, rel, sign, dir = tempdir(), quiet = TRUE, shell = FALSE,
      ...)
```

**Arguments**

mat	The A matrix (see the 4ti2 documentation or examples)
rel	A vector of "<" or ">" relations
sign	The signs of the individual
dir	Directory to place the files in, without an ending /
quiet	If FALSE, messages the 4ti2 output
shell	Messages the shell code used to do the computation
...	Additional arguments to pass to the function

**Value**

The configuration matrix of the model provided

**Examples**

```
if (has_4ti2()) {

  # x + y > 0
  # x + y < 0

  mat <- rbind(
    c( 1,  1),
    c( 1, -1)
  )
  rel <- c(">", "<")
  sign <- c(0, 0)

  qsolve(mat, rel, sign, p = "arb")
  qsolve(mat, rel, sign, p = "arb", quiet = FALSE)
  qsolve(mat, rel, sign, p = "arb", shell = TRUE)

}
```

---

<b>tab2vec</b>	<i>Array to vector conversion</i>
----------------	-----------------------------------

---

## Description

Convert an array into a vector.

## Usage

```
tab2vec(tab)
```

## Arguments

<code>tab</code>	An array of counts
------------------	--------------------

## Details

This function converts an array (or a multi-way contingency table) into a vector, using a consistent ordering of the cells. The ordering of the cells is lexicographical and cannot be specified by the user.

## Value

a Named integer vector. The names correspond to the cell indices in the table.

## See Also

[vec2tab\(\)](#)

## Examples

```
a <- array(1:24, c(2,3,4))
tab2vec(a)
```

```
data(Titanic)
tab2vec(Titanic)
Titanic[1,1,1,1]
Titanic[1,1,1,2]
```

tableau

*Tableau Notation for Markov***Description**

Print the tableau notation for a Markov move. See the reference provided, p. 13.

**Usage**

```
tableau(move, dim)
```

**Arguments**

- |      |   |
|------|---|
| move | a markov move matrix, where the columns are moves in vector form (e.g. the output of <code>markov</code> )          |
| dim  | the dimensions of the table form of the move, oftentimes a vector of the number of levels of each variable in order |

**Value**

an object of class `tableau`

**References**

Drton, M., B. Sturmfels, and S. Sullivant (2009). *Lectures on Algebraic Statistics*, Basel: Birkhauser Verlag AG.

**Examples**

```
vec <- matrix(c(1, -1, -1, 1), nrow = 4)
varlvs <- c(2, 2)
tableau(vec, varlvs)
```

vec2tab

*Vector to array conversion***Description**

Convert a vector into an array given a set of dimensions; it therefore simply wraps `aperm()` and `array()`.

**Usage**

```
vec2tab(vec, dim)
```

**Arguments**

<code>vec</code>	A vector
<code>dim</code>	The desired array dimensions, oftentimes a vector of the number of levels of each variable in order

**Details**

This function converts an array (or a multi-way contingency table) into a vector, using a consistent ordering of the cells. The ordering of the cells is lexicographical and cannot be specified by the user.

**Value**

An array

**See Also**

[tab2vec\(\)](#), [aperm\(\)](#), [array\(\)](#)

**Examples**

```
data(Titanic)
Titanic
tab2vec(Titanic)
vec2tab(tab2vec(Titanic), dim(Titanic))
vec2tab(tab2vec(Titanic), dim(Titanic)) == Titanic
all(vec2tab(tab2vec(Titanic), dim(Titanic)) == Titanic)
```

**zsolve**

*Solve a linear system over the integers*

**Description**

`zsolve` runs 4ti2's `zsolve` program to compute the configuration matrix `A` corresponding to graphical statistical models given by a simplicial complex and levels on the nodes.

**Usage**

```
zsolve(mat, rel, rhs, sign, lat, lb, ub, dir = tempdir(), quiet = TRUE,
      shell = FALSE, ...)
```

**Arguments**

<code>mat</code>	The A matrix (see the 4ti2 documentation or examples)
<code>rel</code>	A vector of "<" or ">" relations
<code>rhs</code>	The right hand side b
<code>sign</code>	The signs of the individual
<code>lat</code>	A lattice basis (instead of a matrix)
<code>lb</code>	Lower bounds on columns
<code>ub</code>	Upper bounds on columns
<code>dir</code>	Directory to place the files in, without an ending /
<code>quiet</code>	If FALSE, messages the 4ti2 output
<code>shell</code>	Messages the shell code used to do the computation
<code>...</code>	Additional arguments to pass to the function

**Value**

The configuration matrix of the model provided

**Examples**

```
if (has_4ti2()) {

  mat <- rbind(
    c( 1, -1),
    c(-3,  1),
    c( 1,  1)
  )
  rel <- c("<", "<", ">")
  rhs <- c(2, 1, 1)
  sign <- c(0, 1)

  zsolve(mat, rel, rhs, sign)
  zsolve(mat, rel, rhs, sign, quiet = FALSE)
  zsolve(mat, rel, rhs, sign, shell = TRUE)

  zsolve(mat, rel, rhs, sign, p = "gmp", quiet = FALSE)

}
```

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