Package 'odr'

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Type Package

Title Optimal Design and Statistical Power for Experimental Studies Investigating Main, Mediation, and Moderation Effects

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Description Calculate the optimal sample size allocation that produces the highest statistical power for experimental studies under a budget constraint, and perform power analyses with and without accommodating cost structures of sampling. The designs cover single-level and multilevel experiments detecting main, mediation, and moderation effects (and some combinations).

The references for the proposed methods include:

(1) Shen, Z., & Kelcey, B. (2020).

Optimal sample allocation under unequal costs in cluster-randomized trials.

Journal of Educational and Behavioral Statistics, 45(4): 446-474. doi:10.3102/1076998620912418>.

(2) Shen, Z., & Kelcey, B. (2022b). Optimal sample allocation for three-level multisite cluster-randomized trials.

Journal of Research on Educational Effectiveness, 15 (1), 130-150. <doi:10.1080/19345747.2021.1953200>.

- (3) Shen, Z., & Kelcey, B. (2022a). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education. <doi:10.1080/00220973.2020.1830361>.
- (4) Champely, S. (2020). pwr: Basic functions for power analysis (Version 1.3-0) [Software]. Available from

<https://CRAN.R-project.org/package=pwr>.

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odr-package	Optimal Design and Statistical Power for Experimental Studies Inves-
, 0	tigating Main, Mediation, and Moderation Effects

Description

This package is to help researchers design cost-efficient and well-powered experimental studies investigating main, mediation, and moderation effects (and some combinations). Specifically, this package can (a) identify optimal sample allocations, (b) compare design efficiency between different sample allocations, and (c) perform power analyses with and without accommodating costs and budget.

Details

The package covers seven types of experiments aiming to detect main, moderation, and mediation effects. These experiments are individual randomized controlled trials (RCTs), two-, three-, and four-level cluster-randomized trials (CRTs), two-, three-, and four-level multisite randomized trials (MRTs). The two categorical functions are 'od' and 'power'. The 'od' function can calculate the optimal sample allocation with and without constraint for each type of experiments. The 'power' function by default can calculate required budget (and required sample size) for desired power, minimum detectable effect size (MDES) under a fixed budget, statistical power under a fixed budget. The 'power' function can perform conventional power analyses (e.g., required sample size, power, MDES calculation). The uniform function 're' (or 'rpe') is to compare the relative (precision and) efficiency between two designs with different sample allocations (limited to main effects).

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gen.design.pars

Generate optimal design parameters using ant colony optimization

Description

This function can generate a set of optimal design parameters based on given distributions of the rank of optimization target (or budget).

```
gen.design.pars(
  dist.mean,
  dist.rank,
  n.of.ants,
  nl,
```

```
q = 1e-04,
n.of.archive = 100,
xi = 0.5
)
```

Arguments

dist.mean	List of means - coordinates
dist.rank	Rank of the archived values of objective function
n.of.ants	Number of ants used in each iteration after the initialization of power analysis for calculating required budget, default value is 10.
nl	Neighborhood of the search area
q	Locality of the search (0,1), default is 0.0001.
n.of.archive	Size of the solution archive, default is 100.
xi	Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.

Value

Generated optimal design parameter value(s) (i.e., a matrix with n.of.ants rows and n.of.design.pars columns)

References

Socha, K., & Dorigo, M. (2008). Ant colony optimization for continuous domains. European Journal of Operational Research, 185(3), 1155-1173.

We thank Dr. Krzysztof Socha for providing us the original code (http://iridia.ulb.ac.be/supp/IridiaSupp2008-001/) for this function.

od.1	Optimal sample allocation calculation for single-level experiments detecting main effects

Description

The optimal design of single-level experiments detecting main effects is to choose the optimal sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameter is the proportion of individuals to be assigned to treatment (p).

Usage

```
od.1(
  p = NULL,
  r12 = NULL,
  c1 = NULL,
  c1t = NULL,
  m = NULL,
  plots = TRUE,
  plim = NULL,
  varlim = NULL,
  varlab = NULL,
  vartitle = NULL,
  verbose = TRUE
)
```

Arguments

р	The proportion of individuals to be assigned to treatment.
r12	The proportion of outcome variance explained by covariates.
c1	The cost of sampling one unit in control condition.
c1t	The cost of sampling one unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 individuals across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
plab	The plot label for ${\sf p}$, default value is "Proportion of Individuals in Treatment: ${\sf p}$ ".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the value of p if TRUE, otherwise not; default value is TRUE.

Value

Unconstrained or constrained optimal sample allocation (p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
myod1$out # output

# Constrained p, no calculation performed #-----
myod2 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2), p = 0.5)</pre>
```

od.1.111

```
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$re # RE = 0.87

# When sampling costs are equal, a balanced design with p = 0.5 is the best #-----
myod3 <- od.1(r12 = 0.5, c1 = 1, c1t = 1, varlim = c(0, 0.2))
myod3$out # output</pre>
```

od.1.111

Optimal sample allocation calculation for single-level randomized controlled trials (RCTs) investigating mediation effects (1-1-1)

Description

The optimal design of single-level RCTs probing mediation effects is to identify the optimal sample allocation that use the minimum budget to achieve a fixed level of statistical power. The optimal design parameter is the proportion of individuals/units to be assigned to the experimental condition. This function identifies the optimal p.

```
od.1.111(
  a = NULL
  b = NULL
  c1 = NULL
  c1t = NULL
 m = NULL,
  r.yx = 0,
  r.mx = 0,
  r.mw = 0,
  q.a = 0,
  q.b = 0,
  test = "joint",
  p = NULL
  n = NULL,
  tol = 1e-11,
  power = 0.8,
  d.p = c(0.1, 0.5),
  sig.level = 0.05,
  two.tailed = TRUE,
  plim = c(0.01, 0.99),
  varlim = c(0, 0.001),
  plab = NULL,
  varlab = NULL,
  vartitle = NULL,
  nlim = c(6, 1e+06),
```

od.1.111

```
verbose = TRUE,
max.value = Inf,
max.iter = 300,
e = 1e-10,
n.of.ants = 10,
n.of.archive = 20,
q = 1e-04,
xi = 0.5
)
```

a	The treatment effect on the mediator.
b	The within-treatment correlation between the outcome and the mediator.
c1	The cost of sampling an individual in the control group.
c1t	The cost of sampling an individual in the treated group.
m	Total budget.
r.yx	The within-treatment correlation between the outcome and the covariate(s) in the outcome model.
r.mx	The within-treatment correlation between the mediator and the covariate(s) in the outcome model.
r.mw	The within-treatment correlation between the mediator and the covariate(s) in the mediator model.
q.a	The number of covariates at the mediator model (except the treatment indicator), the default value is zero.
q.b	The number of covariates in the outcome model (except the treatment indicator and the mediator), the default value is zero.
test	The type of test will be used to detect mediation effects. The default is the joint significance test (i.e., test = "joint", "Joint", "JOINT"). Another choice is the Sobel test by specifying the argument as test = "sobel", "Sobel", or "SOBEL".
р	The proportion of level-4 clusters/units to be assigned to treatment.
n	Total number of individuals in the experimental study, the default value is NULL.
tol	convergence tolerance.
power	Statistical power specified, default is .80.
d.p	The initial sampling domains for p. Default is $c(0.10, 0.50)$.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Two tailed test, the default value is TRUE.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
plab	The plot label for p , default value is "Proportion of Individuals in Treatment: p ".
varlab	The plot label for variance, default value is "Variance".

vartitle	The title of variance plot, default value is NULL.
nlim	The interval/range used to numerically solve for n, the default values are $c(6, 1e7)$.
verbose	Print out evaluation process if TRUE, default is TRUE.
max.value	Maximal value of optimization when used as the stopping criterion. Default is infinite.
max.iter	Maximal number of function evaluations when used as the stopping criterion. Default is 200.
е	Maximum error value used when solution quality used as the stopping criterion, default is 1e-10.
n.of.ants	Number of ants used in each iteration after the initialization stage, the default value is 10.
n.of.archive	Size of the solution archive, default is 20.
q	Locality of the search (0,1), default is 0.0001.
xi	Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.

Value

Unconstrained or constrained optimal sample allocation p). The function also returns statistical power, function name, design type, and parameters used in the calculation.

Examples

```
myod <- od.1.111(a = .3, b = .5, c1 = 10, c1t = 100)
myod
```

od.2	Optimal sample allocation calculation for two-level CRTs detecting main effects

Description

The optimal design of two-level cluster randomized trials (CRTs) detecting main effects is to calculate the optimal sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 clusters/groups to be assigned to treatment (p). This function solves the optimal n and/or p with and without constraints.

Usage

```
od.2(
 n = NULL,
 p = NULL,
 icc = NULL,
 r12 = NULL
 r22 = NULL
 c1 = NULL,
 c2 = NULL,
 c1t = NULL,
 c2t = NULL,
 m = NULL,
 plots = TRUE,
 plot.by = NULL,
 nlim = NULL,
 plim = NULL,
  varlim = NULL,
 nlab = NULL,
 plab = NULL,
 varlab = NULL,
 vartitle = NULL,
  verbose = TRUE
```

n	The level-1 sample size per level-2 unit.
р	The proportion of level-2 clusters/units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 level-2 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n and/or p; default value is plot.by = $list(n = "n", p = "p")$.
nlim	The plot range for n, default value is $c(2, 50)$.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".

plab	The plot label for p, default value is "Proportion Level-2 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446–474. https://doi.org/10.3102/1076998620912418>

Examples

```
# Unconstrained optimal design #-----
 myod1 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              varlim = c(0.01, 0.02))
 myod1$out # output
# Plot by p
 myod1 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              varlim = c(0.01, 0.02), plot.by = list(p = 'p'))
# Constrained optimal design with n = 20 #-----
 myod2 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              n = 20, varlim = c(0.005, 0.025))
 myod2$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre re # RE = 0.88
# Constrained optimal design with p = 0.5 #-----
 myod3 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
 myod3$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod3)</pre>
 myre re # RE = 0.90
# Constrained n and p, no calculation performed #-----
 myod4 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              n = 20, p = 0.5, varlim = c(0.005, 0.025))
 myod4$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod4)
 myre re # RE = 0.83
```

od.2.221

od.2.221

Optimal sample allocation calculation for two-level CRTs probing mediation effects with cluster-level mediators

Description

The optimal design of two-level cluster randomized trials (CRTs) probing mediation effects with cluster-level mediators is to to identify the optimal sample allocation that requires the minimum budget to achieve certain power level. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 clusters/groups to be assigned to treatment (p). This function solves the optimal n and/or p with and without a constraint.

```
od.2.221(
  a = NULL,
 b = NULL,
 n = NULL,
 p = NULL
  icc = NULL,
  c1 = NULL
  c1t = NULL,
  c2 = NULL,
  c2t = NULL,
 m = NULL,
  r2m = 0,
  r.yx = 0,
  r.mw = 0,
  r.yw = 0,
  q.a = 0,
  q.b = 0,
  test = "joint",
  tol = 1e-11,
  power = 0.8,
  d.p = c(0.1, 0.5),
  d.n = c(2, 100),
  sig.level = 0.05,
  two.tailed = TRUE,
  Jlim = c(max(q.a, q.b) + 4, 1e+06),
  verbose = TRUE,
  nrange = c(1.5, 10000),
 max.value = Inf,
 max.iter = 300,
  e = 1e-10,
  n.of.ants = 10,
  n.of.archive = 50,
  q = 1e-04,
```

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```
xi = 0.5
```

а	The treatment effect on the mediator.
b	The within treatment correlation between the outcome and the mediator at the cluster level.
n	The level-1 sample size per level-2 unit.
р	The proportion of level-2 clusters/units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit in control condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
m	Total budget.
r2m	The proportion of mediator variance explained by covariates in the mediator model.
r.yx	The correlation between the outcome and the covariate at the individual level.
r.mw	The correlation between the mediator and the covariate at the cluster level.
r.yw	The correlation between the outcome and the covariate at the cluster level.
q.a	The number of covariates in the mediator model (except the treatment indicator).
q.b	The number of covariates in the outcome model at the cluster level (except the treatment indicator and the mediator).
test	The type of test will be used to detect mediation effects. Default is the joint significance test (i.e., test = "joint"). The other choice is the Sobel test by specifying the argument as test = "sobel".
tol	convergence tolerance.
power	Statistical power specified. The default value is .80.
d.p	The initial sampling domains for p. Default is $c(0.1, 0.5)$.
d.n	The initial sampling domain for n. Default is $c(2, 100)$.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Two tailed test, the default value is TRUE.
Jlim	The range for J to solve for a numerical solution. Default is $c(max(q.a, q.b)+4, 1e6)$.
verbose	Print out evaluation process if TRUE, default is TRUE.
nrange	The range of the individual-level sample size per cluster that used to exclude unreasonable values. Default value is $c(1.5, 10000)$.
max.value	Maximal value of optimization when used as the stopping criterion. Default is -Inf.

od.2m

max.iter	Maximal number of function evaluations when used as the stopping criterion.
е	Maximum error value used when solution quality used as the stopping criterion, default is 1e-10.
n.of.ants	Number of ants used in each iteration after the initialization of power analysis for calculating required budget, default value is 10.
n.of.archive	Size of the solution archive, default is 100.
q	Locality of the search $(0,1)$, default is 0.0001 .
xi	Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of a mediation effect or statistical power, function name, design type, and parameters used in the calculation.

od.2m	Optimal sample allocation calculation for two-level MRTs detecting main effects

Description

The optimal design of two-level multisite randomized trials (MRTs) detecting main effects is to calculate the sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-one sample size per site (n) and the proportion of level-one unit to be assigned to treatment (p). This function solves the optimal n and/or p with and without a constraint.

```
od.2m(
  n = NULL
  p = NULL,
  icc = NULL,
  r12 = NULL
  r22m = NULL,
  c1 = NULL,
  c2 = NULL,
  c1t = NULL,
  omega = NULL,
  m = NULL,
  plots = TRUE,
  plot.by = NULL,
  nlim = NULL,
  plim = NULL,
  varlim = NULL,
```

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```
nlab = NULL,
plab = NULL,
varlab = NULL,
vartitle = NULL,
verbose = TRUE,
iter = 100,
tol = 1e-10
)
```

Arguments

n	The level-1 sample size per level-2 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 sites.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n and/or p; default value is plot.by = $list(n = "n", p = "p")$.
nlim	The plot range for n, default value is c(2, 50).
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
plab	The plot label for p, default value is "Proportion Level-1 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

od.2m.111

References

Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education. https://doi.org/10.1080/00220973.2020.1830361>

Examples

```
# Unconstrained optimal design #-----
 myod1 < - od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005))
 myod1$out # n = 20, p = 0.37
# Plots by p
 myod1 < - od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5.
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), plot.by = list(p = 'p'))
# Constrained optimal design with p = 0.5 \#------
 myod2 < - od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5)
 myod2$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre$re # RE = 0.86
# Constrained optimal design with n = 5 #-----
 myod3 < - od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5, c1 = 1, c2 = 10,
              c1t = 10, varlim = c(0, 0.005), n = 5)
 myod3$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod3)</pre>
 myre re # RE = 0.79
# Constrained n and p, no calculation performed #-----
 myod4 \leftarrow od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5, n = 10)
 myod4$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod4)</pre>
 myre$re # RE = 0.84
```

od.2m.111 Optimal sample allocation calculation for two-level multisiterandomized trials investigating mediation effects with individual-level mediators (1-1-1) od.2m.111

Description

The optimal design of two-level multisite-randomized trials (MRTs) probing mediation effects with individual-level mediators, for the Sobel test, is to calculate the optimal sample allocation that minimizes the variance of a mediation effect under a fixed budget. For the joint significance test, it is to identify the optimal sample allocation that requires the minimum budget to achieve certain power level. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-1 individuals/units to be assigned to treatment (p). This function solves the optimal n and/or p with and without a constraint.

```
od.2m.111(
  a = NULL
  b = NULL,
  icc.m = NULL,
  icc = NULL,
  c1 = NULL
  c1t = NULL
  c2 = NULL,
 m = NULL
  r12m = 0,
  r22m = 0,
  r12 = 0,
  omega = 0.01,
  q.a = 0,
  q.b = 3,
  test = "joint",
  n = NULL,
  p = NULL,
  iter = 100,
  tol = 1e-11,
  power = 0.8,
  d.p = c(0.1, 0.5),
  d.n = c(5, 50),
  sig.level = 0.05,
  two.tailed = TRUE,
  plots = TRUE,
  nlim = c(4, 100),
  plim = c(0.01, 0.99),
  varlim = c(0, 0.001),
  nlab = NULL,
  plab = NULL,
  varlab = NULL,
  vartitle = NULL,
  Jlim = c(3, 1e+05),
  verbose = TRUE,
  max.value = Inf,
  max.iter = 300,
```

od.2m.111

```
e = 1e-10,
n.of.ants = 10,
n.of.archive = 50,
q = 1e-04,
xi = 0.5,
plot.by = list(n = "n", p = "p")
)
```

a	The treatment effect on the mediator.
b	The within treatment correlation between the outcome and the mediator.
icc.m	The intraclass correlation coefficient for the mediator.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit.
m	Total budget.
r12m	The proportion of within treatment mediator variance at the level one explained by covariates.
r22m	The proportion of treatment-by-site variance explained by covariates.
r12	The proportion of within treatment individual-level outcome variance explained by covariates.
omega	The treatment-by-site variance of the outcome.
q.a	The number of covariates at the individual level of the mediator model (except the treatment indicator).
q.b	The number of covariates in the outcome model (except the treatment indicator and the mediator).
test	The type of test will be used to detect mediation effects. Default is the joint significance test (i.e., test = "joint"). Another choice is the Sobel test by specifying the argument as test = "sobel".
n	The level-1 sample size per level-2 unit.
р	The proportion of level-1 units to be assigned to treatment.
iter	number of iteration used for solving roots in the Sobel test.
tol	convergence tolerance.
power	Statistical power specified, default is .80.
d.p	The initial sampling domains for p. Default is $c(0.10, 0.50)$.
d.n	The initial sampling domain for n. Default is c(4, 500).
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.

plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
nlim	The plot range for n, default value is $c(2, 50)$.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
plab	The plot label for p, default value is "Proportion Level-3 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
Jlim	The range for J to search for a numerical solution. Default is c(3, 10e4).
verbose	Print out evaluation process if TRUE, default is TRUE.
max.value	Maximal value of optimization when used as the stopping criterion. Default is infinite.
max.iter	Maximal number of function evaluations when used as the stopping criterion. Default is 200.
e	Maximum error value used when solution quality used as the stopping criterion, default is 1e-10.
n.of.ants	Number of ants used in each iteration after the initialization of power analysis for calculating required budget, default value is 10.
n.of.archive	Size of the solution archive, default is 100.
q	Locality of the search (0,1), default is 0.0001.
xi	Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.
plot.by	Plot the variance by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns statistical power, function name, design type, and parameters used in the calculation.

od.3	Optimal sample allocation calculation for three-level CRTs detecting
	main effects

Description

The optimal design of three-level cluster randomized trials (CRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), and the proportion of level-3 clusters/groups to be assigned to treatment (p). This function solves the optimal n, J and/or p with and without constraints.

Usage

```
od.3(
  n = NULL,
  J = NULL,
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32 = NULL,
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c1t = NULL,
  c2t = NULL,
  c3t = NULL,
  m = NULL,
  plots = TRUE,
  plot.by = NULL,
  nlim = NULL,
  Jlim = NULL,
  plim = NULL,
  varlim = NULL,
  nlab = NULL,
  Jlab = NULL,
  plab = NULL,
  varlab = NULL,
  vartitle = NULL,
  verbose = TRUE,
  iter = 100,
  tol = 1e-10
)
```

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
p	The proportion of level-3 clusters/units assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2 .
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3 .
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.

c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
m	Total budget, default is the total costs of sampling 60 level-3 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J and/or p; default is plot.by = list(n = "n", J = "J", p = "p").
nlim	The plot range for n, default value is $c(2, 50)$.
Jlim	The plot range for J, default value is $c(2, 50)$.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
plab	The plot label for p, default is "Proportion Level-3 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, and p if TRUE, otherwise not; default is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446–474. https://doi.org/10.3102/1076998620912418

Examples

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```
# Constrained optimal design with J = 20 #-----
     myod2 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
                                        c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
                                        varlim = c(0, 0.025))
     myod2$out
# Relative efficiency (RE)
     myre <- re(od = myod1, subod= myod2)</pre>
     myre re # RE = 0.53
# Constrained optimal design with p = 0.5 #-----
     myod3 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, p = 0.5,
                                        c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
                                        varlim = c(0.005, 0.025))
     myod3$out
# Relative efficiency (RE)
     myre <- re(od = myod1, subod= myod3)</pre>
     myrere # RE = 0.84
# Constrained n, J and p, no calculation performed #------
   myod4 \leftarrow 0.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, n = 10, J = 10, p = 0.5, r32 = 0.5, r32
                                        c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
                                        varlim = c(0, 0.025))
     myod4$out
# Relative efficiency (RE)
     myre <- re(od = myod1, subod= myod4)</pre>
     myre re # RE = 0.61
```

od.3m

Optimal sample allocation calculation for three-level MRTs detecting main effects

Description

The optimal design of three-level multisite randomized trials (MRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), and the proportion of level-2 unit to be assigned to treatment (p). This function solves the optimal n, J and/or p with and without constraints.

```
od.3m(
    n = NULL,
    J = NULL,
    p = NULL,
    icc2 = NULL,
    icc3 = NULL,
```

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```
r12 = NULL
 r22 = NULL,
 r32m = NULL,
 c1 = NULL,
 c2 = NULL,
 c3 = NULL,
 c1t = NULL,
 c2t = NULL,
 omega = NULL,
 m = NULL,
 plots = TRUE,
 plot.by = NULL,
 nlim = NULL,
  Jlim = NULL,
 plim = NULL,
  varlim = NULL,
 nlab = NULL,
  Jlab = NULL,
 plab = NULL,
 varlab = NULL,
 vartitle = NULL,
 verbose = TRUE,
  iter = 100,
  tol = 1e-10
)
```

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 level-3 units.

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plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J and/or p; default value is plot.by = list(n = "n", J = "J", p = "p").
nlim	The plot range for n, default value is $c(2, 50)$.
Jlim	The plot range for J, default value is c(2, 50).
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
plab	The plot label for p, default value is "Proportion Level-2 Units in Treatment: p ".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2022). Optimal sampling ratios in three-level multisite experiments. Journal of Research on Educational Effectiveness.

Examples

```
# Unconstrained optimal design #-----
 myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32m = 0.5,
             c1 = 1, c2 = 5,
             c1t = 1, c2t = 200, c3 = 200,
             varlim = c(0, 0.005))
 myod1$out # output
# Plots by p and J
 myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32m = 0.5,
             c1 = 1, c2 = 5,
             c1t = 1, c2t = 200, c3 = 200,
             varlim = c(0, 0.005), plot.by = list(p = 'p', J = 'J'))
\# Constrained optimal design with p = 0.5 \#-----
 myod2 < - od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32m = 0.5,
             c1 = 1, c2 = 5,
```

```
c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5)
 myod2$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre re # RE = 0.81
# Constrained optimal design with n = 5 #-----
 myod3 < - od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), n = 5)
 myod3$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod3)</pre>
 myre re # RE = 0.89
# Constrained n, J and p, no calculation performed #------
 myod4 < - od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5, n = 15, J = 20)
 myod4$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod4)</pre>
 myre re # RE = 0.75
```

Optimal sample allocation calculation for four-level CRTs detecting main effects

Description

od.4

The optimal design of four-level cluster randomized trials (CRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-4 clusters/groups to be assigned to treatment (p). This function solves the optimal n, J, K and/or p with and without constraints.

```
od.4(
n = NULL,
J = NULL,
```

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```
K = NULL
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  icc4 = NULL,
  r12 = NULL,
 r22 = NULL,
 r32 = NULL,
 r42 = NULL,
 c1 = NULL,
 c2 = NULL,
 c3 = NULL,
  c4 = NULL,
 c1t = NULL,
  c2t = NULL,
  c3t = NULL,
  c4t = NULL,
 m = NULL,
 plots = TRUE,
 plot.by = NULL,
 nlim = NULL,
  Jlim = NULL,
 Klim = NULL,
  plim = NULL,
 varlim = NULL,
 nlab = NULL,
  Jlab = NULL,
 Klab = NULL,
 plab = NULL,
 varlab = NULL,
  vartitle = NULL,
  verbose = TRUE,
  iter = 100,
  tol = 1e-10
)
```

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3 .
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4 .
r12	The proportion of level-1 variance explained by covariates.

r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42	The proportion of level-4 variance explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c 3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
c4t	The cost of sampling one level-4 unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 level-4 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	The plot range for n, default value is $c(2, 50)$.
Jlim	The plot range for J, default value is $c(2, 50)$.
Klim	The plot range for K, default value is $c(2, 50)$.
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
Klab	The plot label for K, default value is "Level-3 Sample Size: K".
plab	The plot label for p, default value is "Proportion Level-4 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, K, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

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Examples

```
# Unconstrained optimal design #-----
 myod1 < - od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01))
 myod1$out # output
# Plots by p and K
 myod1 < - od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01), plot.by = list(p = 'p', K = 'K'))
# Constrained optimal design with p = 0.5 #-----
 myod2 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, p = 0.5,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01))
 myod2$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myrere # RE = 0.78
# Constrained optimal design with K = 20 #-----
 myod3 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, K = 20,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01))
 myod3$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod3)</pre>
 myre re # RE = 0.67
# Constrained n, J, K and p, no calculation performed #------
 myod4 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
              r12 = 0.5, n = 10, J = 10, K = 20, p = 0.5,
              r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01))
 myod4$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod4)</pre>
 myre re # RE = 0.27
```

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Optimal sample allocation calculation for four-level MRTs detecting main effects

Description

The optimal design of four-level multisite randomized trials (MRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-3 units to be assigned to treatment (p). This function solves the optimal n, J, K and/or p with and without constraints.

```
od.4m(
  n = NULL,
  J = NULL
 K = NULL
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  icc4 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32 = NULL,
  r42m = NULL
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c4 = NULL,
  c1t = NULL,
  c2t = NULL,
  c3t = NULL,
  omega = NULL,
 m = NULL,
  plots = TRUE,
  plot.by = NULL,
  nlim = NULL,
  Jlim = NULL,
 Klim = NULL,
  plim = NULL,
  varlim = NULL,
  nlab = NULL,
  Jlab = NULL,
 Klab = NULL,
```

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```
plab = NULL,
varlab = NULL,
vartitle = NULL,
verbose = TRUE,
iter = 100,
tol = 1e-10
)
```

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-3 units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 level-4 units.
plots	$Logical, provide\ variance\ plots\ if\ TRUE,\ otherwise\ not;\ default\ value\ is\ TRUE.$
plot.by	Plot the variance by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	The plot range for n, default value is $c(2, 50)$.
Jlim	The plot range for J, default value is $c(2, 50)$.
Klim	The plot range for K, default value is c(2, 50).
plim	The plot range for p, default value is $c(0, 1)$.
varlim	The plot range for variance, default value is $c(0, 0.05)$.
nlab	The plot label for n, default value is "Level-1 Sample Size: n".

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Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
Klab	The plot label for K, default value is "Level-3 Sample Size: K".
plab	The plot label for p, default value is "Proportion Level-3 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, K, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

Examples

```
# Unconstrained optimal design #-----
 myod1 < - od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005))
 myod1$out # output
# Plots by p and K
 myod1 < - od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), plot.by = list(p = 'p', K = 'K'))
\# Constrained optimal design with p = 0.5 \#-----
 myod2 < - od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), p = 0.5)
 myod2$out
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre$re # RE = 0.88
# Constrained optimal design with J = 20 #-----
 myod3 < - od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005), J = 20)
```

power.1

power.1

Budget and/or sample size, power, MDES calculation for single-level experiments detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for single-level experiments. It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

```
power.1(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL
  power = NULL,
 m = NULL,
  n = NULL,
  p = NULL
  r12 = NULL,
 q = NULL,
  c1 = NULL
  c1t = NULL,
  dlim = NULL,
  powerlim = NULL,
  nlim = NULL,
 mlim = NULL,
```

power.1

```
rounded = TRUE
)
```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned object from function od.1; default value is NULL; if expr is specified, parameter values of r12, c1, c1t, and p used or solved in function od.1 will be passed to the current function; only the value of p that specified or solved in function od.1 can be overwritten if constraint is specified.
constraint	Specify the constrained value of p in list format to overwrite that from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The total sample size.
р	The proportion of individuals to be assigned to treatment.
r12	The proportion of outcome variance explained by covariates.
q	The number of covariates.
c1	The cost of sampling one unit in control condition.
c1t	The cost of sampling one unit in treatment condition.
dlim	The range for solving the root of effect size (d) numerically, default value is $c(0, 5)$.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
nlim	The range for searching the root of sample size (n) numerically, default value is $c(4, 10e10)$.
mlim	The range for searching the root of budget (m) numerically, default value is the costs sampling nlim units across treatment conditions or $c(4 * ncost, 10e10 * ncost)$ with $ncost = ((1 - p) * c1 + p * c1t)$.
rounded	Logical; round p that is from functions od.1 to two decimal places if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

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Examples

```
# Unconstrained optimal design
 myod1 \leftarrow od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
 myod1$out # p = 0.31
# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
 mym.1 < - power.1(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1$out # m = 1032 n = 461
 # mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 mym.1 \leftarrow power.1(d = 0.2, power = 0.8, c1 = 1, c1t = 5,
                 r12 = 0.5, p = 0.31, q = 1)
# Required budget and sample size with constrained p
 mym.2 \leftarrow power.1(expr = myod1, d = 0.2, q = 1, power = 0.8,
              constraint = list(p = 0.5))
 mym.2$out # m = 1183, n = 394
# Power calculation
 mypower <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032,
               constraint = list(p = 0.5))
 mypower.1$out # power = 0.74
# MDES calculation
 mymdes <- power.1(expr = myod1, q = 1, power = 0.80, m = 1032)
 mymdes$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size n
 myn <- power.1(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myn$out # n = 461
 # myn$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myn <- power.1(cost.model = FALSE, d = 0.2, power = 0.8,
                  r12 = 0.5, p = 0.31, q = 1)
# Power calculation
 mypower1 \leftarrow power.1(cost.model = FALSE, expr = myod1, n = 461, d = 0.2, q = 1)
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 <- power.1(cost.model = FALSE, expr = myod1, n = 461, power = 0.8, q = 1)
 mvmdes1$out # d = 0.20
```

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power.1.111

Budget and/or sample size, power, MDES calculation for MRTs investigating mediation effects with individual-level mediators

Description

This function can calculate required budget for desired power and power under a fixed budget for multisite-randomized trials (MRTs) with individual mediators probing mediation effects. It also can perform conventional power analyses (e.g., required sample size and power calculation).

Usage

```
power.1.111(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  a = NULL
 b = NULL,
 power = NULL,
 m = NULL
  test = NULL,
 n = NULL,
  p = NULL,
  c1 = NULL
  c1t = NULL,
  r.yx = 0,
  r.mx = 0,
  r.mw = 0,
  q.a = 0,
  q.b = 0,
 max.iter = 300,
  alim = c(0, 4),
 blim = c(0.01, 0.99),
 powerlim = NULL,
 nlim = c(6, 1e+07),
 mlim = NULL
)
```

Arguments

cost.model

Logical; power analyses accommodating costs and budget (e.g., required budget for a desired power, power under fixed budget) if TRUE. Otherwise, conventional power analyses are performed (e.g., required sample size and power calculation); default value is TRUE.

expr

Returned object from function od.1.111; default value is NULL; if expr is specified, parameter values of a, b, c, ct, and p used or solved in function

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	od.1.111 will be passed to the current function; only the values of p that specified or solved in function od.1.111 can be overwritten if constraint is specified.
constraint	If specified, the constrained value of p in a list format (e.g., constraint = $list(p = 0.5)$) will overwrite that from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Two tailed test, the default value is TRUE.
a	The treatment effect on the mediator.
b	The within-treatment correlation between the outcome and the mediator.
power	Statistical power specified, default is .80.
m	Total budget.
test	The type of test will be used to detect mediation effects. The default is the NULL or the one used in the expr Choices are the joint significance test (i.e., test = "joint", "Joint", "JOINT") or the Sobel test (test = "sobel", "Sobel", or "SOBEL").
n	Total number of individuals in the experimental study, the default value is NULL.
р	The proportion of level-4 clusters/units to be assigned to treatment.
c1	The cost of sampling an individual in the control group.
c1t	The cost of sampling an individual in the treated group.
r.yx	The within-treatment correlation between the outcome and the $covariate(s)$ in the outcome model.
r.mx	The within-treatment correlation between the mediator and the covariate(s) in the outcome model.
r.mw	The within-treatment correlation between the mediator and the covariate(s) in the mediator model.
q.a	The number of covariates at the mediator model (except the treatment indicator), the default value is zero.
q.b	The number of covariates in the outcome model (except the treatment indicator and the mediator), the default value is zero.
max.iter	Maximal number of function evaluations when used as the stopping criterion. Default is 200.
alim	The range for identifying the root of a path effect (a) numerically. Default value is $c(0,4)$.
blim	The range for identifying the root of b path within-treatment correlation between the mediator and outcome (b) numerically. Default value is (.01, .99), if (b) is negative, please re-code the outcome or mediator to make it positive.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
nlim	The interval/range used to numerically solve for n , the default values are $c(6, 1e7)$.
mlim	The range for identifying the root of budget (m) numerically, default value is the costs sampling $nlim$ units.

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Value

Required budget (or required sample size), statistical power, (a), or (b) depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

Examples

power.2

Budget and/or sample size, power, MDES calculation for two-level CRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

```
power.2(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  p = NULL,
  icc = NULL,
  r12 = NULL,
```

```
r22 = NULL,
q = NULL,
c1 = NULL,
c2 = NULL,
c1t = NULL,
d1im = NULL,
powerlim = NULL,
Jlim = NULL,
mlim = NULL,
rounded = TRUE
```

Arguments

cost.model Logical; power analyses accommodating costs and budget (e.g., required bud-

get for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES cal-

culation); default value is TRUE.

expr Returned object from function od. 2; default is NULL; if expr is specified, pa-

rameter values of icc, r12, r22, c1, c2, c1t, c2t, n, and p used or solved in function od.2 will be passed to the current function; only the values of n and p that specified or solved in function od.2 can be overwritten if constraint is

specified.

constraint Specify the constrained values of n and/or p in list format to overwrite those

from expr; default is NULL.

sig. level Significance level or type I error rate, default value is 0.05.

two.tailed Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is

TRUE.

d Effect size.

power Statistical power. m Total budget.

n The level-1 sample size per level-2 unit.

J The total level-2 sample size.

p The proportion of level-2 clusters/units to be assigned to treatment.

icc The unconditional intraclass correlation coefficient (ICC) in population or in

each treatment condition.

r12 The proportion of level-1 variance explained by covariates.

The proportion of level-2 variance explained by covariates.

q The number of level-2 covariates.

c1 The cost of sampling one level-1 unit in control condition.

c2 The cost of sampling one level-2 unit in control condition.

c1t The cost of sampling one level-1 unit in treatment condition.

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c2t	The cost of sampling one level-2 unit in treatment condition.
dlim	The range for solving the root of effect size (d) numerically, default value is $c(0, 5)$.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e\text{-}10, 1\text{-}1e\text{-}10)$.
Jlim	The range for searching the root of level-2 sample size (J) numerically, default is $c(4, 10e10)$.
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling Jlim level-2 units across treatment conditions or $c(4*Jcost, 10e10*Jcost)$, with $Jcost = ((1-p)*(c1*n+c2)+p*(c1t*n+c2t))$.
rounded	Logical; round n and p that are from functions od . 2 to integer and two decimal places, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446–474. https://doi.org/10.3102/1076998620912418

```
# Unconstrained optimal design
 myod1 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50)
 myod1$out # n = 8.9, p = 0.33
# ----- Power analyses by default considering costs and budget ------
# Required budget and sample size
 mym.1 < -power.2(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1$out # m = 3755, J = 130.2
 \#mym.1\$par \# parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 mym.1 \leftarrow power.2(d = 0.2, power = 0.8, icc = 0.2,
                 c1 = 1, c2 = 5, c1t = 1, c2t = 50,
                  r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)
# Required budget and sample size with constrained p
 mym.2 < -power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
               constraint = list(p = 0.5))
 mym.2$out # m = 4210, J = 115.3
# Required budget and sample size with constrained p and n
 mym.3 \leftarrow power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
               constraint = list(p = 0.5, n = 20))
 mym.3sout # m = 4568, J = 96.2
# Power calculation
 mypower <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755)
```

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```
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755,
               constraint = list(p = 0.5))
 mypower.1$out # power = 0.75
# MDES calculation
 mymdes <- power.2(expr = myod1, q = 1, power = 0.80, m = 3755)
 mymdes\$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required J
 myJ <- power.2(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myJ$out # J = 130.2
 #myJ$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myJ \leftarrow power.2(cost.model = FALSE, d = 0.2, power = 0.8, icc = 0.2,
                  r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)
# Power calculation
 mypower1 <- power.2(cost.model = FALSE, expr = myod1, J = 130, d = 0.2, q = 1)</pre>
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 \leftarrow power.2(cost.model = FALSE, expr = myod1, J = 130, power = 0.8, q = 1)
 mymdes1$out # d = 0.20
```

power.2.221

Budget and/or sample size, power calculation for CRTs probing mediation effects with cluster-level mediators

Description

This function can calculate required budget for desired power and power under a fixed budget for experimental studies with group mediators probing mediation effects. It also can perform conventional power analyses (e.g., required sample size and power calculation).

Usage

```
power.2.221(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  a = NULL,
  b = NULL,
```

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```
test = "joint",
  n = NULL,
  p = NULL
  power = NULL,
  J = NULL
 m = NULL,
  c1 = NULL
  c1t = NULL
  c2 = NULL.
  c2t = NULL
  r2m = r2m,
  r.yx = 0,
  r.mw = 0,
  r.yw = 0,
  icc = NULL,
  q = 0,
  q.a = 0,
  q.b = 0,
  powerlim = NULL,
  Jlim = NULL,
 mlim = NULL
)
```

Arguments

cost.model Logical; power analyses accommodating costs and budget (e.g., required bud-

get for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES cal-

culation); default value is TRUE.

expr returned object from function od.2.221; default value is NULL; if expr is

specified, parameter values of a, b, c1, c1t, and p used or solved in function od.2.221 will be passed to the current function; only the values of p and n that specified or solved in function od.2.221 can be overwritten if constraint is

specified.

constraint specify the constrained value of p and/or n in a list format to overwrite that/those

from expr; default value is NULL.

sig. level Significance level or type I error rate, default value is 0.05.

two.tailed Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is

TRUE.

a The treatment effect on the mediator.

b The within treatment correlation between the outcome and the mediator at the

cluster level.

The type of test will be used to detect mediation effects. Default is the joint sig-

nificance test (i.e., test = "joint"). The other choice is the Sobel test by specifying

the argument as test = "sobel".

n The level-1 sample size per level-2 unit.

p	The proportion of level-2 clusters/units to be assigned to treatment.
power	Statistical power.
J	The total level-2 sample size.
m	Total budget.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit in control condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
r2m	The proportion of mediator variance explained by covariates in the mediator model.
r.yx	The correlation between the outcome and the covariate at the individual level.
r.mw	The correlation between the mediator and the covariate at the cluster level.
r.yw	The correlation between the outcome and the covariate at the cluster level.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
q	The number of level-2 covariates.
q.a	The number of covariates in the mediator model (except the treatment indicator).
q.b	The number of covariates in the outcome model at the cluster level (except the treatment indicator and the mediator).
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e\text{-}10, 1\text{-}1e\text{-}10)$.
Jlim	The range for searching the root of level-2 sample size (J) numerically, default is $c(4,10e10)$.
mlim	the range for searching the root of budget (m) numerically, default value is the costs sampling nlim units across treatment conditions or c(4 * ncost, 10e10 * ncost) with ncost = $((1 - p) * c1 + p * c1t)$

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

power.2m	Budget and/or sample size, power, MDES calculation for two-level
	MRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.2m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
 m = NULL,
  n = NULL,
  J = NULL,
  p = NULL
  icc = NULL,
  r12 = NULL,
 r22m = NULL,
  q = NULL,
  c1 = NULL
  c2 = NULL,
  c1t = NULL
 omega = NULL,
  dlim = NULL,
  powerlim = NULL,
  Jlim = NULL,
 mlim = NULL,
  rounded = TRUE
)
```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required bud-
	get for desired power, power/MDES under fixed budget) if TRUE, otherwise
	conventional power analyses (a.g. required sample size power or MDES cal

conventional power analyses (e.g., required sample size, power, or MDES cal-

culation); default value is TRUE.

expr Returned objects from function od.2m; default is NULL; if expr is specified,

parameter values of icc, r12, r22m, c1, c2, c1t, p, and n used or solved in function od.2m will be passed to current function; only the values of p and n that specified or solved in function od.2m can be overwritten if constraint is

specified.

constraint Specify the constrained values of p and/or n in list format to overwrite those

from expr; default value is NULL.

sig.level Significance level or type I error rate, default value is 0.05.

two.tailed Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is

TRUE.

d Effect size.

power Statistical power.

m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The number of sites.
р	The proportion of level-1 units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22m	The proportion of variance of site-specific treatment effect explained by covariates.
q	The number of covariates at level 2.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for solving the root of effect size (d) numerically, default value is $c(0, 5)$.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
Jlim	The range for searching the root of level-2 sample size (J) numerically, default is $c(4, 10e10)$.
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling J1im level-2 units or $c(4 * Jcost, 1e+10 * Jcost)$ with $Jcost = (1 - p) * c1 * n + p * c1t * n + c2$.
rounded	Logical; round the values of p, $n/J/K$ that are from functions od. 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education. https://doi.org/10.1080/00220973.2020.1830361>

```
# ----- Power analyses by default considering costs and budget ------
# Required budget and sample size
 mym.1 \leftarrow power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1$out # m = 2019, J = 20.9
 # mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 mym.1 < -power.2m(d = 0.2, power = 0.8, q = 1,
                 icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
                 c1 = 1, c2 = 10, c1t = 10,
                 n = 20, p = 0.37
# Required budget and sample size with constrained p
 mym.2 \leftarrow power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
 mym.2sout # m = 2373, J = 19.8
# Required budget and sample size with constrained p and n
 mym.3 \leftarrow power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 5))
 mym.3sout # m = 2502, J = 66.7
# Power calculation
 mypower <- power.2m(expr = myod1, q = 1, d = 0.2, m = 2019)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.2m(expr = myod1, q = 1, d = 0.2, m = 2019,
                 constraint = list(p = 0.5))
 mypower.1$out # power = 0.72
# MDES calculation
 mymdes <- power.2m(expr = myod1, q = 1, power = 0.80, m = 2019)
 mymdes$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
 myJ \leftarrow power.2m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myJ$out # J = 6.3
 # myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myJ <- power.2m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
                 icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
                 c1 = 1, c2 = 10, c1t = 10,
                 n = 20, p = 0.37
# Power calculation
 mypower1 \leftarrow power.2m(cost.model = FALSE, expr = myod1, J = 6.3, d = 0.2, q = 1)
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 <- power.2m(cost.model = FALSE, expr = myod1, J = 6.3, power = 0.8, q = 1)</pre>
 mymdes1$out # d = 0.20
```

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power.2m.111

Budget and/or sample size, power, MDES calculation for MRTs investigating mediation effects with individual-level mediators

Description

This function can calculate required budget for desired power and power under a fixed budget for multisite-randomized trials (MRTs) with individual mediators probing mediation effects. It also can perform conventional power analyses (e.g., required sample size and power calculation).

Usage

```
power.2m.111(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  a = NULL,
  b = NULL
  power = NULL,
 m = NULL
  test = NULL,
  n = NULL,
  p = NULL
  c1 = NULL,
  c1t = NULL
  c2 = NULL,
  r12 = 0,
  r22m = 0,
  r12m = 0,
  icc.m = NULL,
  omega = NULL,
  icc = NULL,
  J = NULL,
  q = 0,
  q.a = 0,
  q.b = 0,
 max.iter = 300,
  powerlim = NULL,
  Jlim = NULL,
 mlim = NULL,
  rounded = TRUE
)
```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned object from function od.2m.111; default value is NULL; if expr is specified, parameter values of a, b, c1, c1t, and p used or solved in function od.2m.111 will be passed to the current function; only the values of p and n that specified or solved in function od.2m.111 can be overwritten if constraint is specified.
constraint	specify the constrained value of p and/or n in a list format to overwrite that/those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
а	The treatment effect on the mediator.
b	The within treatment correlation between the outcome and the mediator.
power	Statistical power.
m	Total budget.
test	The type of test will be used to detect mediation effects. Default is the joint significance test (i.e., test = "joint"). Another choice is the Sobel test by specifying the argument as test = "sobel".
n	The level-1 sample size per level-2 unit.
p	The proportion of level-1 units to be assigned to treatment.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit.
r12	The proportion of level-1 variance explained by covariates.
r22m	The proportion of variance of site-specific treatment effect explained by covariates.
r12m	The proportion of within treatment mediator variance at the level one explained by covariates.
icc.m	The intraclass correlation coefficient for the mediator.
omega	The standardized variance of site-specific treatment effect.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
J	The number of sites.
q	The number of covariates at level 2.
q.a	The number of covariates at the individual level of the mediator model (except the treatment indicator).

q.b	The number of covariates in the outcome model (except the treatment indicator and the mediator).
max.iter	Maximal number of function evaluations when used as the stopping criterion. Default is 200.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
Jlim	The range for searching the root of level-2 sample size (J) numerically, default is $c(4, 10e10)$.
mlim	the range for searching the root of budget (m) numerically, default value is the costs sampling nlim units.
rounded	Logical; round the values of p, n/J/K that are from functions od . 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

power.3	Budget and/or sample size, power, MDES calculation for three-level CRTs detecting main effects
	CRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.3(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  L = NULL,
  J = NULL,
  K = NULL,
  p = NULL,
  icc2 = NULL,
```

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```
icc3 = NULL,
  r12 = NULL,
  r22 = NULL
  r32 = NULL,
  q = NULL,
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c1t = NULL
  c2t = NULL,
  c3t = NULL,
  dlim = NULL,
  powerlim = NULL,
 Klim = NULL,
 mlim = NULL,
  rounded = TRUE
)
```

Arguments

		_			
cost.model	Logical nower	analyees accor	mmodating coete	and budget (e.g.,	required bud
COSt. MOUEL	Logical, power	anaryses accor	innouating costs	and budget (c.g.,	, required bud-

get for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES cal-

culation); default value is TRUE.

expr Returned objects from function od.3; default is NULL; if expr is specified,

parameter values of icc2, icc3, r12, r22, r32, c1, c2, c3, c1t, c2t, c3t, p, n, and J used or solved in function od.3 will be passed to the current function; only the values of p, n, and/or J that specified or solved in function od.3 can be

overwritten if constraint is specified.

constraint Specify the constrained values of p, n, and/or J in list format to overwrite those

from expr; default is NULL.

sig.level Significance level or type I error rate, default value is 0.05.

two.tailed Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is

TRUE.

d Effect size.

power Statistical power. m Total budget.

n The level-1 sample size per level-2 unit.

J The level-2 sample size per level-3 unit.

K The total level-3 sample size.

p The proportion of level-3 clusters/units assigned to treatment.

icc2 The unconditional intraclass correlation coefficient (ICC) at level 2. icc3 The unconditional intraclass correlation coefficient (ICC) at level 3.

r12 The proportion of level-1 variance explained by covariates.

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r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
q	The number of covariates at level 3.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
dlim	The range for solving the root of effect size (d) numerically, default value is c(0, 5).
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
Klim	The range for searching the root of level-3 sample size (K) numerically, default value is $c(4, 1e+10)$.
mlim	The range for searching the root of budget (m) numerically, default value is the costs sampling K1im level-3 units across treatment conditions or $c(4 * Kcost, 1e+10 * Kcost)$ with $Kcost = ((1 - p) * (c1 * n * J + c2 * J + c3) + p * (c1t * n * J + c2t * J + c3t))$.
rounded	Logical; round the values of p, n/J that are from functions od. 3 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446-474. https://doi.org/10.3102/1076998620912418>

```
# Unconstrained optimal design
 myod1 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250)
 myod1$out # output # n = 7.9, J = 3.2, p = 0.28
# ----- Power analyses by default considering costs and budget ------
# Required budget and sample size
 mym.1 \leftarrow power.3(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1$out # m = 16032, K = 97.3
 #mym.1$par # parameters and their values used for the function
```

```
# Or, equivalently, specify every argument in the function
 mym.1 \leftarrow power.3(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
                 c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
                 n = 8, J = 3, p = 0.28)
# Required budget and sample size with constrained p
 mym.2 < -power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
 mym.2sout # m = 19239, K = 78.8
# Required budget and sample size with constrained p and J
 mym.3 \leftarrow power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, J = 20))
 mym.3$out # m = 39774, K = 46.9
# Power calculation
 mypower \leftarrow power.3(expr = myod1, q = 1, d = 0.2, m = 16032)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.3(expr = myod1, q = 1, d = 0.2, m = 16032,
                 constraint = list(p = 0.5))
 mypower.1$out # power = 0.72
# MDES calculation
 mymdes <- power.3(expr = myod1, q = 1, power = 0.80, m = 16032)
 mymdes$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
 myK <- power.3(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myK$out # K = 97.3
 \mbox{\tt \#myK\$par} \mbox{\tt \#} parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myK <- power.3(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
                  icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
                  n = 8, J = 3, p = 0.28)
# Power calculation
 mypower1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, d = 0.2, q = 1)</pre>
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, power = 0.8, q = 1)
 mymdes1$out # d = 0.20
```

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.3m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
 m = NULL
 n = NULL,
  J = NULL
 K = NULL
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32m = NULL,
  q = NULL,
  c1 = NULL
  c2 = NULL,
  c3 = NULL,
 c1t = NULL,
  c2t = NULL,
  omega = NULL,
  dlim = NULL,
  powerlim = NULL,
 Klim = NULL,
 mlim = NULL,
  rounded = TRUE
)
```

Arguments

cost.model

Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.

expr

Returned objects from function od.3m; default is NULL; if expr is specified, parameter values of icc2, icc3, r12, r22, r32m, c1, c2, c3, c1t, c2t, p, n, and J used or solved in function od.3m will be passed to current function; only

	the values of p, n, and/or J that specified or solved in function od.3m can be overwritten if constraint is specified.
constraint	Specify the constrained values of p, n, and/or J, in list format to overwrite those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-2 units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32m	The proportion of variance of site-specific treatment effect explained by covariates.
q	The number of covariates at level 3.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for solving the root of effect size (d) numerically, default value is $c(0, 5)$.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e-10, 1-1e-10)$.
Klim	The range for searching the root of level-3 sample size (K) numerically, default value is c(4, 1e+10).
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling Klim level-3 units or $c(4 * Kcost, 1e+10 * Kcost)$ with $Kcost = ((1 - p) * (c1 * n * J + c2 * J) + p * (c1t * n * J + c2t * J) + c3.$
rounded	Logical; round the values of p, n/J/K that are from functions od . 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. Journal of Research on Educational Effectiveness.

```
# Unconstrained optimal design #-----
 myod1 < - od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005))
 myod1$out # n = 13.1, J = 15.3, p = 0.23
# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
 mym.1 \leftarrow power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1sout # m = 15491, K = 13.6
 # mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 mym.1 < -power.3m(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, omega = 0.02,
                  r12 = 0.5, r22 = 0.5, r32m = 0.5,
                  c1 = 1, c2 = 5,
                  c1t = 1, c2t = 200, c3 = 200,
                  n = 13, J = 15, p = 0.23)
# Required budget and sample size with constrained p
 mym.2 \leftarrow power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
 mym.2$out # m = 21072, K = 10.9
# Required budget and sample size with constrained p and n
 mym.3 \leftarrow power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
 mym.3sout # m = 21252, K = 10.4
# Power calculation
 mypower <- power.3m(expr = myod1, q = 1, d = 0.2, m = 15491)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.3m(expr = myod1, q = 1, d = 0.2, m = 15491,
                 constraint = list(p = 0.5))
 mypower.1$out # power = 0.62
# MDES calculation
 mymdes \leftarrow power.3m(expr = myod1, q = 1, power = 0.80, m = 15491)
 mymdes$out # d = 0.20
```

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```
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
 myK <- power.3m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myK$out # K = 13.6
 # myK$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myK \leftarrow power.3m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
                  icc2 = 0.2, icc3 = 0.1, omega = 0.02,
                  r12 = 0.5, r22 = 0.5, r32m = 0.5,
                  c1 = 1, c2 = 5,
                  c1t = 1, c2t = 200, c3 = 200,
                  n = 13, J = 15, p = 0.23)
# Power calculation
 mypower1 <- power.3m(cost.model = FALSE, expr = myod1, K = 13.6, d = 0.2, q = 1)
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 \leftarrow power.3m(cost.model = FALSE, expr = myod1, K = 13.6, power = 0.8, q = 1)
 mymdes1$out # d = 0.20
```

power.4

Budget and/or sample size, power, MDES calculation for four-level CRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.4(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  L = NULL,
  L = NULL,
```

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```
p = NULL,
 icc2 = NULL,
 icc3 = NULL,
 icc4 = NULL,
 r12 = NULL,
 r22 = NULL,
 r32 = NULL,
 r42 = NULL
 q = NULL,
 c1 = NULL,
 c2 = NULL,
 c3 = NULL,
 c4 = NULL,
 c1t = NULL,
 c2t = NULL,
 c3t = NULL,
 c4t = NULL,
 dlim = NULL,
 powerlim = NULL,
 Llim = NULL,
 mlim = NULL,
 rounded = TRUE
)
```

Arguments

Κ

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function od.4; default value is NULL; if expr is specified, parameter values of icc2, icc3, icc4, r12, r22, r32, r42, c1, c2, c3, c4, c1t, c2t, c3t, c4t, p, n, J, and K used or solved in function od.4 will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function od.4 can be overwritten if constraint is specified.
constraint	Specify the constrained values of p, n, J, and/or K in list format to overwrite those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.

The level-3 sample size per level-4 unit.

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L	The total level-4 sample size.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42	The proportion of level-4 variance explained by covariates.
q	The number of covariates at level 4.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
c4t	The cost of sampling one level-4 unit in treatment condition.
dlim	The range for solving the root of effect size (d) numerically, default value is $c(0, 5)$.
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e\text{-}10, 1\text{-}1e\text{-}10)$.
Llim	The range for solving the root of level-4 sample size (L) numerically, default value is $c(4, 1e+10)$.
mlim	The range for searching the root of budget (m) numerically, default value is the costs sampling Llim level-4 units across treatment conditions or $c(4 * Lcost, 1e+10 * Lcost)$ with Lcost = $((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K + c4) + p * (c1t * n * J * K + c2t * J * K + c3t * K + c4t)$.
rounded	Logical; round the values of p, $n/J/K$ that are from functions od . 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

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```
# Unconstrained optimal design
 myod1 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500)
 myod1$out # output # n = 7.1, J = 3.2, K = 4.2, p = 0.23
# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
 mym.1 \leftarrow power.4(expr = myod1, d = 0.2, q = 1, power = 0.8)
 mym.1$out # m = 71161, L = 57.1
 #mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 mym.1 \leftarrow power.4(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
                 r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
                 c1 = 1, c2 = 5, c3 = 25, c4 = 125,
                 c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
                 n = 7, J = 3, K = 4, p = 0.23)
# Required budget and sample size with constrained p (p = 0.5)
 mym.2 < -power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
 mym.2$out # m = 93508, L = 41.1
# Required budget and sample size with constrained p and K
 mym.3 \leftarrow power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, K = 20))
 mym.3$out # m = 157365, L = 25.7
# Power calculation
 mypower <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161,
                 constraint = list(p = 0.5))
 mypower.1$out # power = 0.68
# MDES calculation
 mymdes <- power.4(expr = myod1, q = 1, power = 0.80, m = 71161)
 mymdes$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
 myL \leftarrow power.4(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myL$out # L = 57.1
#myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myL <- power.4(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
                  r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
                  n = 7, J = 3, K = 4, p = 0.23)
```

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```
# Power calculation
  mypower1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, d = 0.2, q = 1)
  mypower1$out # power = 0.80

# MDES calculation
  mymdes1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, power = 0.8, q = 1)
  mymdes1$out # d = 0.20</pre>
```

power.4m

Budget and/or sample size, power, MDES calculation for four-level MRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.4m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL
 power = NULL,
 m = NULL,
 n = NULL.
  J = NULL
 K = NULL
 L = NULL,
 p = NULL
 icc2 = NULL,
  icc3 = NULL,
  icc4 = NULL,
  r12 = NULL,
 r22 = NULL
  r32 = NULL,
  r42m = NULL,
 q = NULL,
  c1 = NULL,
 c2 = NULL,
  c3 = NULL,
  c4 = NULL,
```

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```
c1t = NULL,
c2t = NULL,
c3t = NULL,
omega = NULL,
dlim = NULL,
powerlim = NULL,
Llim = NULL,
mlim = NULL,
rounded = TRUE
)
```

Arguments

cost.model Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise

conventional power analyses (e.g., required sample size, power, or MDES cal-

culation); default value is TRUE.

expr Returned objects from function od. 4m; default is NULL; if expr is specified,

parameter values of icc2, icc3, icc4, r12, r22, r32, r42m, c1, c2, c3, c4, c1t, c2t, c3t, p, n, J, and K used or solved in function od. 4m will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function

od. 4m can be overwritten if constraint is specified.

constraint The constrained values of p, n, J, and/or K in list format to overwrite those from

expr; default value is NULL.

sig.level Significance level or type I error rate, default value is 0.05.

two.tailed Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is

TRUE.

d Effect size.

power Statistical power. m Total budget.

n The level-1 sample size per level-2 unit.

J The level-2 sample size per level-3 unit.

K The level-3 sample size per level-4 unit.

L The total level-4 sample size.

p The proportion of level-3 units to be assigned to treatment.

icc2 The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3 The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4 The unconditional intraclass correlation coefficient (ICC) at level 4.

r12 The proportion of level-1 variance explained by covariates. r22 The proportion of level-2 variance explained by covariates.

The proportion of level-3 variance explained by covariates.

r42m The proportion of variance of site-specific treatment effect explained by covari-

ates.

power.4m

q	The number of covariates at level 4.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for solving the root of effect size (d) numerically, default value is c(0, 5).
powerlim	The range for solving the root of power (power) numerically, default value is $c(1e\text{-}10, 1\text{-}1e\text{-}10)$.
Llim	The range for solving the root of level-4 sample size (L) numerically, default value is $c(4, 1e+10)$.
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling Llim level-4 units or c(4 * Lcost, 1e+10 * Lcost) with Lcost = ((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K) + p * (c1t * n * J * K + c2t * J * K + c3t * K) + c4.
rounded	Logical; round the values of p, $n/J/K$ that are from functions od . 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

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```
icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
                 r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
                 c1 = 1, c2 = 5, c3 = 25,
                 c1t = 1, c2t = 50, c3t = 250, c4 = 500,
                 n = 8, J = 3, K = 5, p = 0.36)
# Required budget and sample size with constrained p
 mym.2 \leftarrow power.4m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
 mym.2sout # m = 33183, L = 19.3
# Required budget and sample size with constrained p and n
 mym.3 \leftarrow power.4m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
 mym.3$out # m = 34262, L = 18.0
# Power calculation
 mypower \leftarrow power.4m(expr = myod1, q = 1, d = 0.2, m = 30201)
 mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
 mypower.1 <- power.4m(expr = myod1, q = 1, d = 0.2, m = 30201,
                 constraint = list(p = 0.5))
 mypower.1$out # power = 0.76
# MDES calculation
 mymdes <- power.4m(expr = myod1, q = 1, power = 0.80, m = 30201)
 mymdes$out # d = 0.20
# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
 myL \leftarrow power.4m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
 myL$out # L = 20.6
 # myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
 myL <- power.4m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
                 r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
                 c1 = 1, c2 = 5, c3 = 25,
                 c1t = 1, c2t = 50, c3t = 250, c4 = 500,
                 n = 8, J = 3, K = 5, p = 0.36)
# Power calculation
 mypower1 <- power.4m(cost.model = FALSE, expr = myod1, L = 20.6, d = 0.2, q = 1)
 mypower1$out # power = 0.80
# MDES calculation
 mymdes1 <- power.4m(cost.model = FALSE, expr = myod1, L = 20.6, power = 0.8, q = 1)
 mymdes1$out # d = 0.20
```

fe re

Description

Calculate the relative efficiency (RE) between two designs, it returns same results as those from function rpe.

Usage

```
re(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od	Returned object of first design (e.g., unconstrained optimal design) from function od.1, od.2, od.3, od.4, od.2m, od.3m, or od.4m.
subod	Returned object of second design (e.g., constrained optimal design) from function od.1, od.2, od.3, od.4, od.2m, od.3m, or od.4m.
rounded	Logical; round the values of p, n/J/K that are from functions to two decimal places and integer, respectively if TRUE, no rounding if FALSE; default is TRUE.
verbose	Logical; print the value of relative efficiency if TRUE, otherwise not; default is TRUE.

Value

Relative efficiency value.

References

(1) Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446–474. https://doi.org/10.3102/107699862091 (2) Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education. https://doi.org/10.1080/00220973.2020.1830361 (3) Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. Journal of Research on Educational Effectiveness.

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```
myre re # RE = 0.90
# Unconstrained optimal design of 3-level CRT #------
 myod1 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# Constrained optimal design with J = 20
 myod2 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre re # RE = 0.53
# Unconstrained optimal design of 4-level CRT #------
 myod1 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
              r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01))
# Constrained optimal design with p = 0.5
 myod2 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
              r22 = 0.5, r32 = 0.5, r42 = 0.5,
              c1 = 1, c2 = 5, c3 = 25, c4 = 125,
              c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
              varlim = c(0, 0.01)
# Relative efficiency (RE)
 myre <- re(od = myod1, subod= myod2)</pre>
 myre re # RE = 0.78
```

Relative precision and efficiency (RPE) calculation

Description

rpe

Calculate the relative precision and efficiency (RPE) between two designs, it returns same results as those from function re.

Usage

```
rpe(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od Returned object of first design (e.g., unconstrained optimal design) from function od. 1, od. 2, od. 3, od. 4, od. 2m, od. 3m, or od. 4m.

Subod Returned object of second design (e.g., constrained optimal design) from function od. 1, od. 2, od. 3, od. 4, od. 2m, od. 3m, or od. 4m.

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rounded Logical; round the values of p, n/J/K that are from functions to two decimal

places and integer, respectively if TRUE, no rounding if FALSE; default is

TRUE.

verbose Logical; print the value of relative precision and efficiency if TRUE, otherwise

not; default is TRUE.

Value

Relative precision and efficiency value.

References

(1) Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. Journal of Educational and Behavioral Statistics, 45(4): 446–474. https://doi.org/10.3102/107699862091 (2) Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education. https://doi.org/10.1080/00220973.2020.1830361 (3) Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. Journal of Research on Educational Effectiveness.

```
# Unconstrained optimal design of 2-level CRT #-----
 myod1 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              varlim = c(0.01, 0.02)
# Constrained optimal design with n = 20
 myod2 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
              n = 20, varlim = c(0.005, 0.025))
# Relative precision and efficiency (RPE)
 myrpe <- rpe(od = myod1, subod= myod2)</pre>
 myrpe$rpe # RPE = 0.88
# Constrained optimal design with p = 0.5
 myod2 \leftarrow od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
# Relative precision and efficiency (RPE)
 myrpe <- rpe(od = myod1, subod= myod2)</pre>
 myrpe$rpe # RPE = 0.90
# Unconstrained optimal design of 3-level CRT #------
 myod1 \leftarrow od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# Constrained optimal design with J = 20
 myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# Relative precision and efficiency (RPE)
 myrpe <- rpe(od = myod1, subod= myod2)</pre>
 myrpe$rpe # RPE = 0.53
# Unconstrained optimal design of 4-level CRT #------
 myod1 \leftarrow od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
```

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```
r22 = 0.5, r32 = 0.5, r42 = 0.5,
c1 = 1, c2 = 5, c3 = 25, c4 = 125,
c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
varlim = c(0, 0.01))

# Constrained optimal design with p = 0.5
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
r22 = 0.5, r32 = 0.5, r42 = 0.5,
c1 = 1, c2 = 5, c3 = 25, c4 = 125,
c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
varlim = c(0, 0.01))

# Relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod= myod2)
myrpe$rpe # RPE = 0.78
```

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